

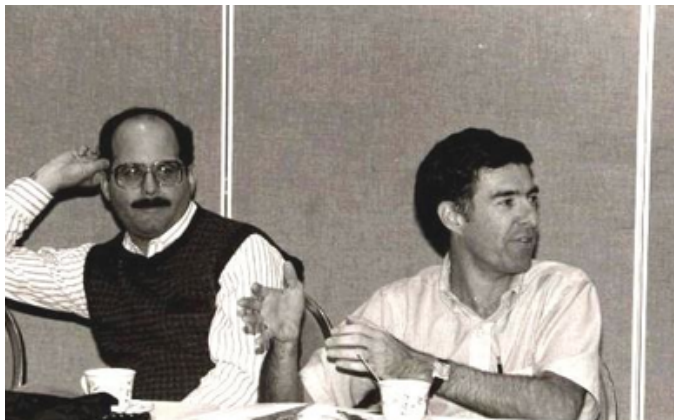
Image Registration for Remote Sensing

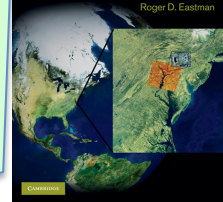
Jacqueline Le Moigne

Nathan S. Netanyahu

Roger D. Eastman

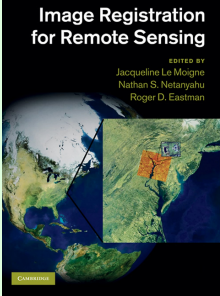
A Few Memories, 1983 to 1988 ...





Around CVL, 1983 to 1988 ...





Context and Background

Jacqueline Le Moigne

NASA Goddard Space Flight Center

Image Registration

in the Context of Space Missions

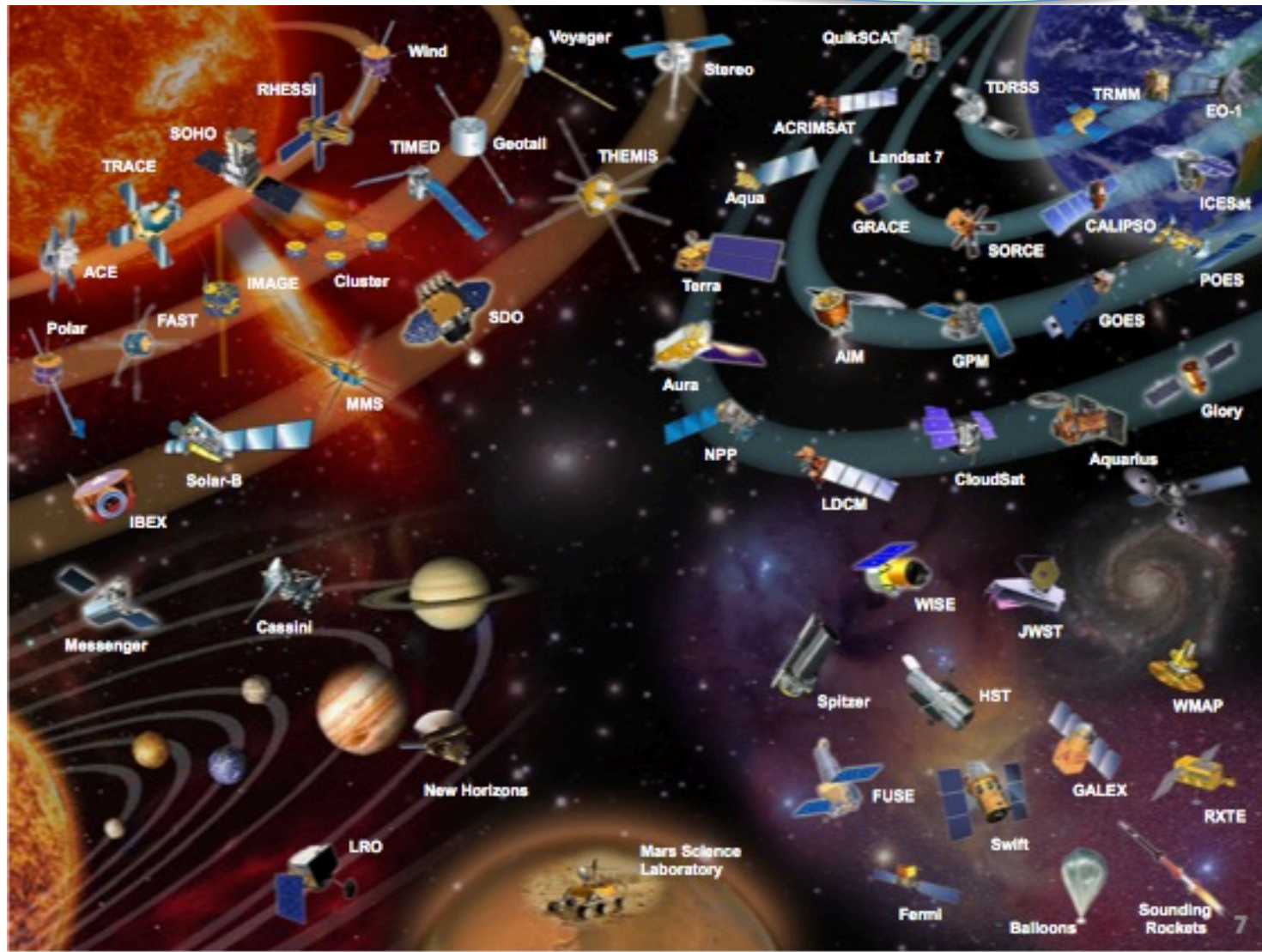
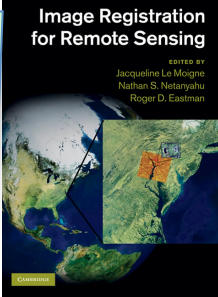


Image Registration in the Context of Earth Remote Sensing



Earth Science



NASA pioneered the interdisciplinary field of Earth System Science—the study of the Earth as an integrated system. This approach to studying the Earth as a single complex system is essential to understanding the causes and consequences of climate change and other global environmental concerns. Spaceborne instruments provide essential broad coverage, high spatial resolution, frequent sampling, and near-uniform accuracy and stability. Multiple on-orbit missions, including those flying in coordinated orbits as part of planned constellations, allow data to be acquired simultaneously on many important quantities, enabling investigations of the interactions among the coupled Earth processes that constitute the climate system. NASA's research, coupled with that of our partners in the U.S. Global Change Research Program, provides much of the nation's knowledge base for understanding, mitigating, and adapting to climate change.

Advance Earth System Science
to meet the challenges of climate
and environmental change.

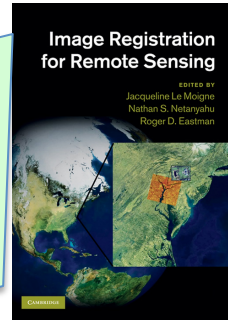


Spatial and Spectral Characteristics of Some Operational Sensors (Ch. 14-22)



Instrument (Spat. Resol.)	Number of Channels	Wavelength (µm)																									
		0.1	0.4	0.5	0.6	0.7	1.0	1.3	2.0	3.0	4.0	5.0	6.0	7.0	8.0	9.0	10.0	11.0	12.0	13.0	14.0	15.0					
AVHRR (1.1 km)	5 Channels			1) 0.58-0.68		1		2		2) 0.725-1.10		3) 3.55-3.93		3		4) 10.3-11.3		4		5		5) 11.5-12.5					
GOES (1 km:1, 4km:2,4&5, 8km:3)	5 Channels			1) 0.55-0.75		1				2) 3.80-4.00		2		3) 6.50-7.00		3		4) 10.2-11.2		4		5		5) 11.5-12.5			
IKONOS (4 m)	4 Channels				1	2		3		4		1) 0.445-0.516		2) 0.506-0.595		3) 0.632-0.698		4) 0.757-0.853									
IKONOS Panchromatic (1 m)					Pan				1) 0.45-0.90																		
Landsat5&7/ TM&ETM+ (30 m, except Ch6: 120 m)	7 Channels			1	2		3		4		5		7		1) 0.45-0.52		2) 0.52-0.60		3) 0.63-0.69		4) 0.75-0.90		5) 1.55-1.75		6) 2.09-2.35		6) 10.4-12.5
Landsat7-Panchromatic (15 m)					Pan				1) 0.52-0.90																		
METEOSAT (V:2.5km,WV&IR:5km)	3 Channels	V) 0.4-1.1	Visible											WV) 5.7-7.1										IR) 10.5-12.5		IR	
MISR (275 m to 1.1 km)	4 channels x 9 cameras = 36			1	2		3		4		1) 0.443		2) 0.555		3) 0.670		4) 0.865										
MODIS (Ch1-2:250 m;3-7:500m;8-36:1km)		1) 0.62-0.67 2) 0.84-0.88 3) 0.46-0.48 4) 0.55-0.57 5) 1.33-1.25 6) 1.63-1.65 7) 2.11-2.16	3, 8-10	11, 4, 12	1, 13,1 4	15	2, 16- 19	5	26	6	7	8) 0.41-0.42 9) 0.44-0.45 10) 0.48-0.49 11) 0.53-0.54 12) 0.55-0.56 13) 0.66-0.67 14) 0.67-0.68 15) 0.74-0.75 16) 0.86-0.88	20-25	17) 0.89-0.92 18) 0.93-0.94 19) 0.92-0.97 20) 3.66-3.84 21) 3.93-3.99 22) 3.93-3.99 23) 4.02-4.08 24) 4.43-4.50 25) 4.48-4.55 26) 1.36-1.39	27	28	29	30	31	32	33-36	27) 6.5-6.9 28) 7.2-7.5 29) 8.4-8.7 30) 9.6-9.9 31) 10.8-11.3 32) 11.8-12.3 33) 13.2-13.5 34) 13.5-13.8 35) 13.8-14.1 36) 14.1-14.4					
SeaWiFS (1.1 km)	8 Channels		1	2	3	4	5		1) 0.43-0.45		2) 0.51-0.53		3) 0.54-0.56		4) 0.66-0.68		5) 0.70-0.80		6		6) 10.5-12.5						
SPOT5-HRV Panchromatic (5 m)	1 Channel				Pan				1) 0.51-0.73																		
Spot5-HRG (10 m, except Ch.4: 20 m)	4 Channels			1) 0.5-0.59		1		2		3		4		2) 0.61-0.68		3) 0.79-0.89		4) 1.58-1.75									
VEGETATION (1.165 km)	4 Channels			1) 0.43-0.47		1		2		3		4		2) 0.61-0.68		3) 0.79-0.89		4) 1.58-1.75									

What is Image Registration ...



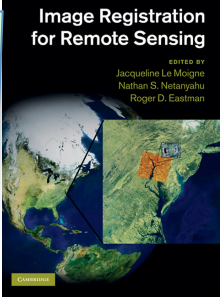
- Definition

“Exact pixel-to-pixel matching of two different images or matching of one image to a map”

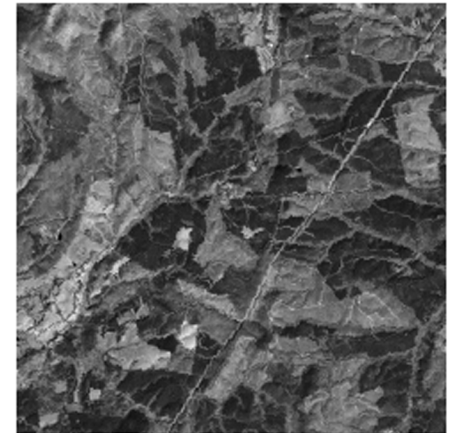
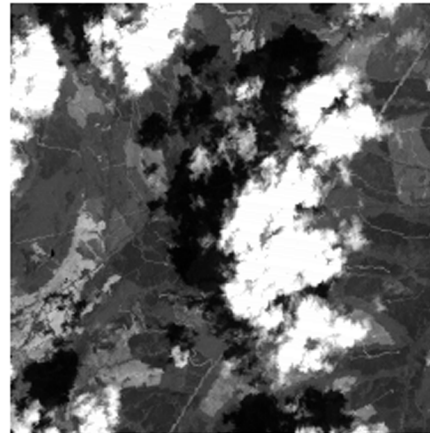
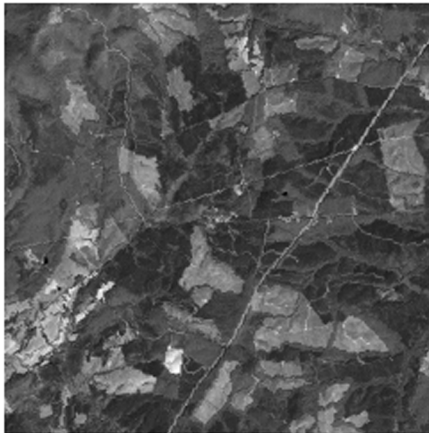
- Multiple Source Data

- Multimodal Registration
- Temporal Registration
- Viewpoint Registration
- Template Registration

Challenges in Image Registration for Remote Sensing

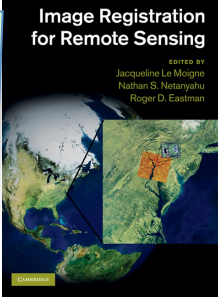


- Remote Sensing vs. Medical or Other Imagery
 - Variety in the types of sensor data and the conditions of data acquisition
 - Size of the data
 - Lack of a known image model
 - Lack of well-distributed “fiducial points” resulting in lack of algorithms validation
- Navigation Error
- Atmospheric and Cloud Interactions

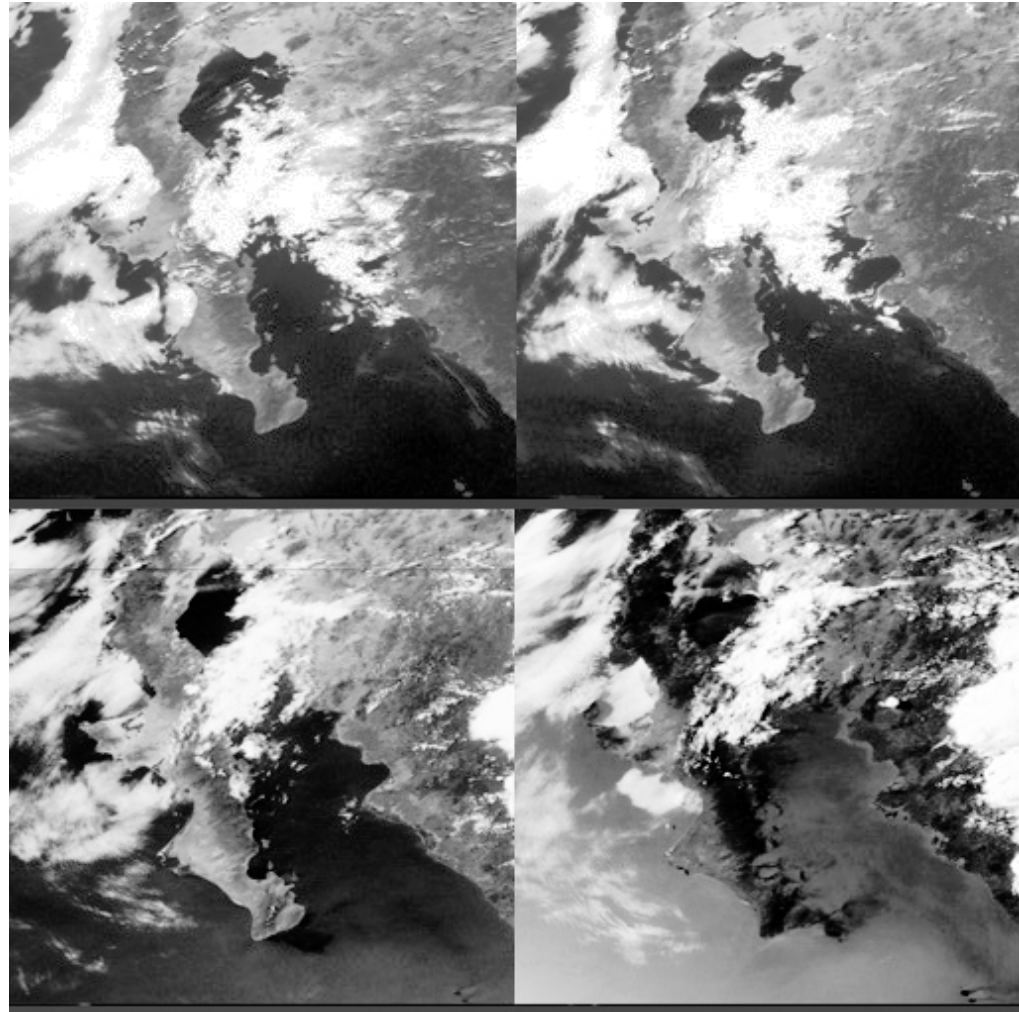


*Three Landsat images over Virginia acquired in August, October, and November 1999
(Courtesy: Jeffrey Masek, NASA Goddard Space Flight Center)*

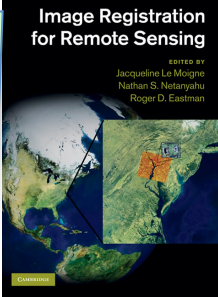
Challenges in Image Registration for Remote Sensing



**Atmospheric and
Cloud Interactions**
*Baja Peninsula,
California; 4 different
times of the day (GOES-8)*
(Reproduced from Le Moigne &
Eastman, 2005)



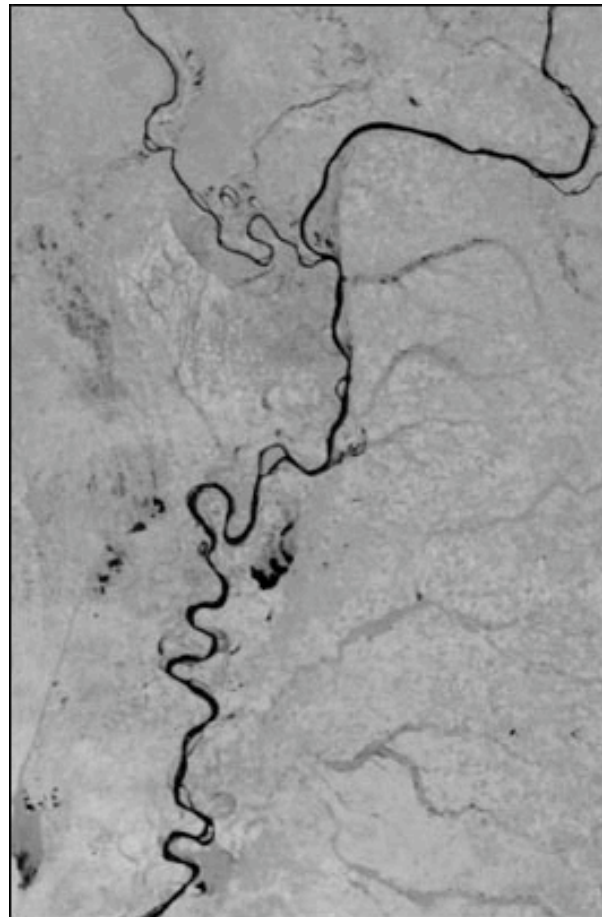
Challenges in Image Registration for Remote Sensing



Multitemporal Effects

*Mississippi and Ohio
Rivers before & after
Flood of Spring 2002
(Terra/MODIS)*

(Reproduced from Le Moigne &
Eastman, 2005)

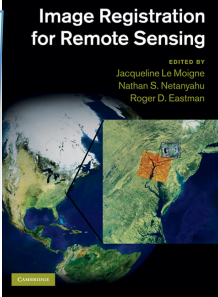


April 25, 2002



May 18, 2002

Challenges in Image Registration for Remote Sensing



Relief Effect
SAR and Landsat-TM
Data of Lopé Area,
Gabon, Africa
(Reproduced from Le
Moigne & Eastman, 2005)

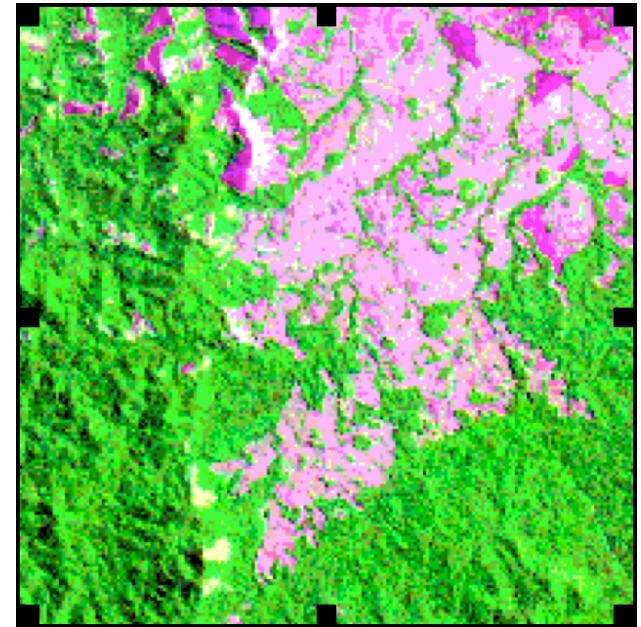
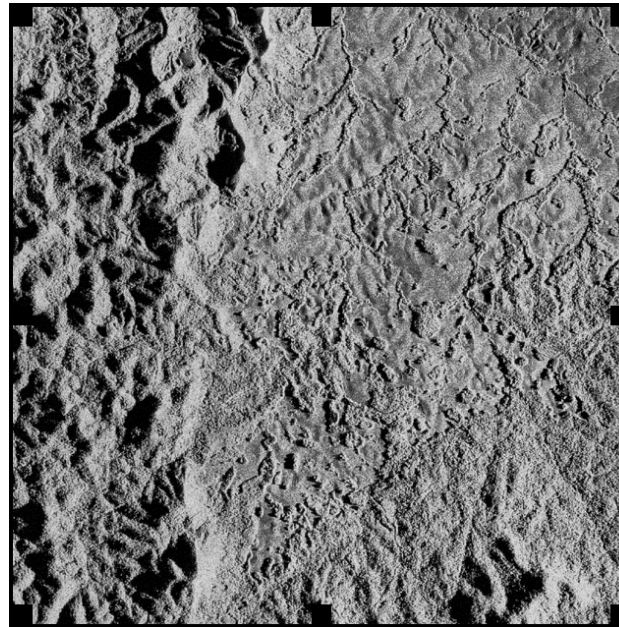
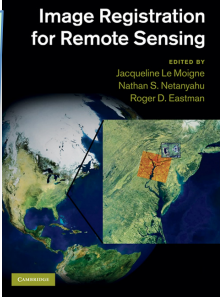
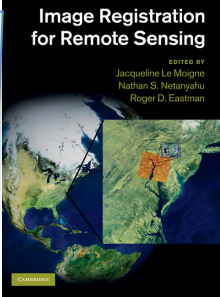


Image Registration or Precision Correction



- Navigation or Model-Based Systematic Correction
 - Orbital, Attitude, Platform/Sensor Geometric Relationship, Sensor Characteristics, Earth Model, etc.
- Image Registration/Feature-Based Precision Correction
 - Navigation within a Few Pixels Accuracy
 - Image Registration Using Selected Features (or Control Points) to Refine Geo-Location Accuracy
- Image Registration as a Post-Processing or as a Feedback to Navigation Model

Misregistration



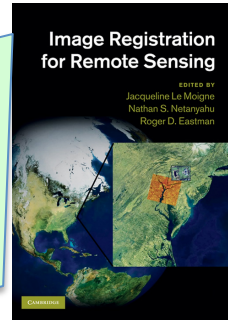
- (Townshead et al, 1992) and (Dai & Khorram, 1998): small error in registration may have a large impact on global change measurements accuracy
- e.g., 1 pixel misregistration error => 50% error in Vegetation Index (NDVI) computation (using 250m MODIS data)



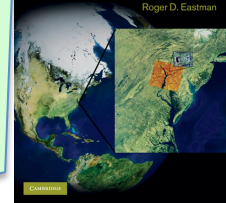
*Human-induced land cover changes observed by Landsat-5 in Bolivia in 1984 and 1998
(Courtesy: Compton J. Tucker **and** the Landsat Project, NASA Goddard Space Flight Center)*

- Influence of image registration on products validation
- Impact of misregistration on legal, economic and sociopolitical (e.g., resource management), etc.

Image Registration Frameworks



- **Mathematical Framework**
 - $I_1(x,y)$ and $I_2(x,y)$: images or image/map
 - find the mapping (f,g) which transforms I_1 into I_2 : $I_2(x,y) = g(I_1(fx(x,y),fy(x,y)))$
 - » f : spatial mapping
 - » g : radiometric mapping
 - **Spatial Transformations “f”**
 - Translation, Rigid, Affine, Projective, Perspective, Polynomial, ...
 - **Radiometric Transformations “g” (Resampling)**
 - Nearest Neighbor, Bilinear, Cubic Convolution, ...
- **Algorithmic Framework (Brown, 1992)**
 1. Feature Extraction
 2. Feature Matching
 3. Image Resampling



NASA Goddard Image Registration Group

- 1994: First results on the utilization of orthogonal Daubechies wavelets for image registration



Figure 1
Original Image

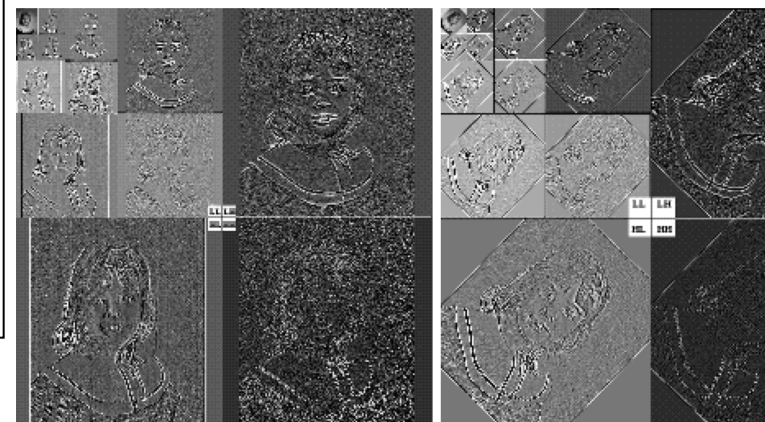
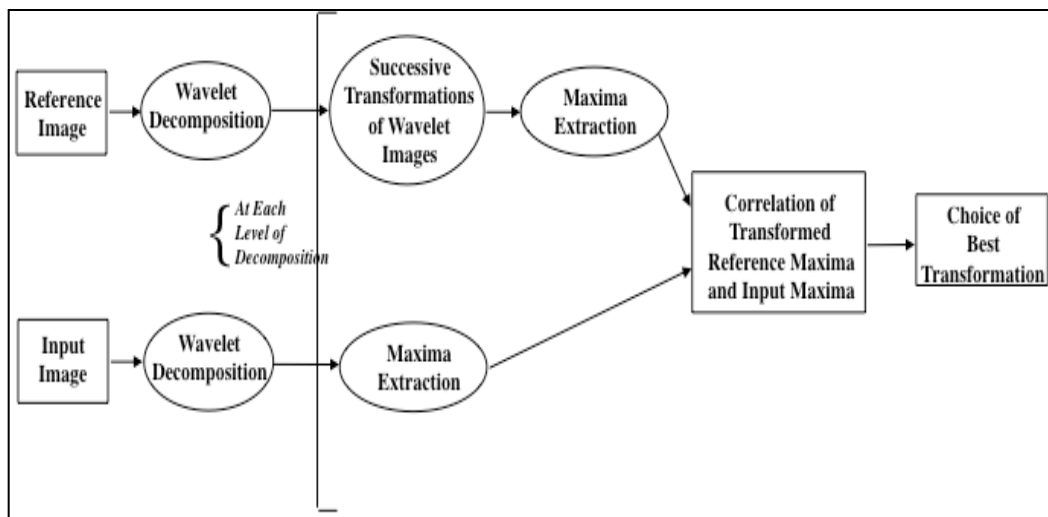
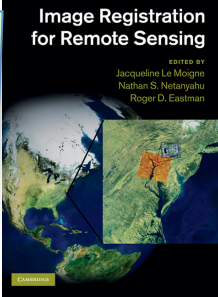


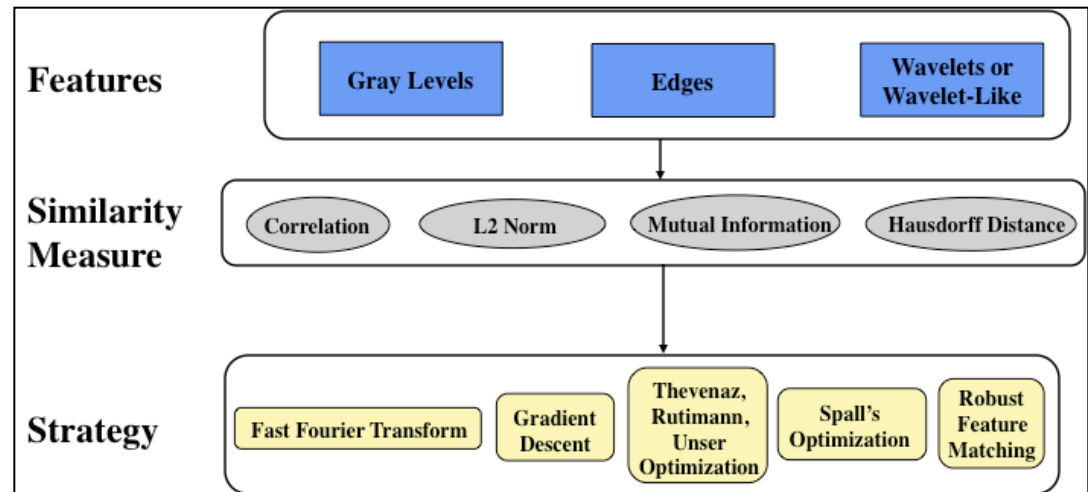
Figure 2
Wavelet Coefficients Corresponding to Figure 1

Figure 3
Wavelet Coefficients Correspond to Figure 1 rotated 44 degrees



NASA Goddard Image Registration Group

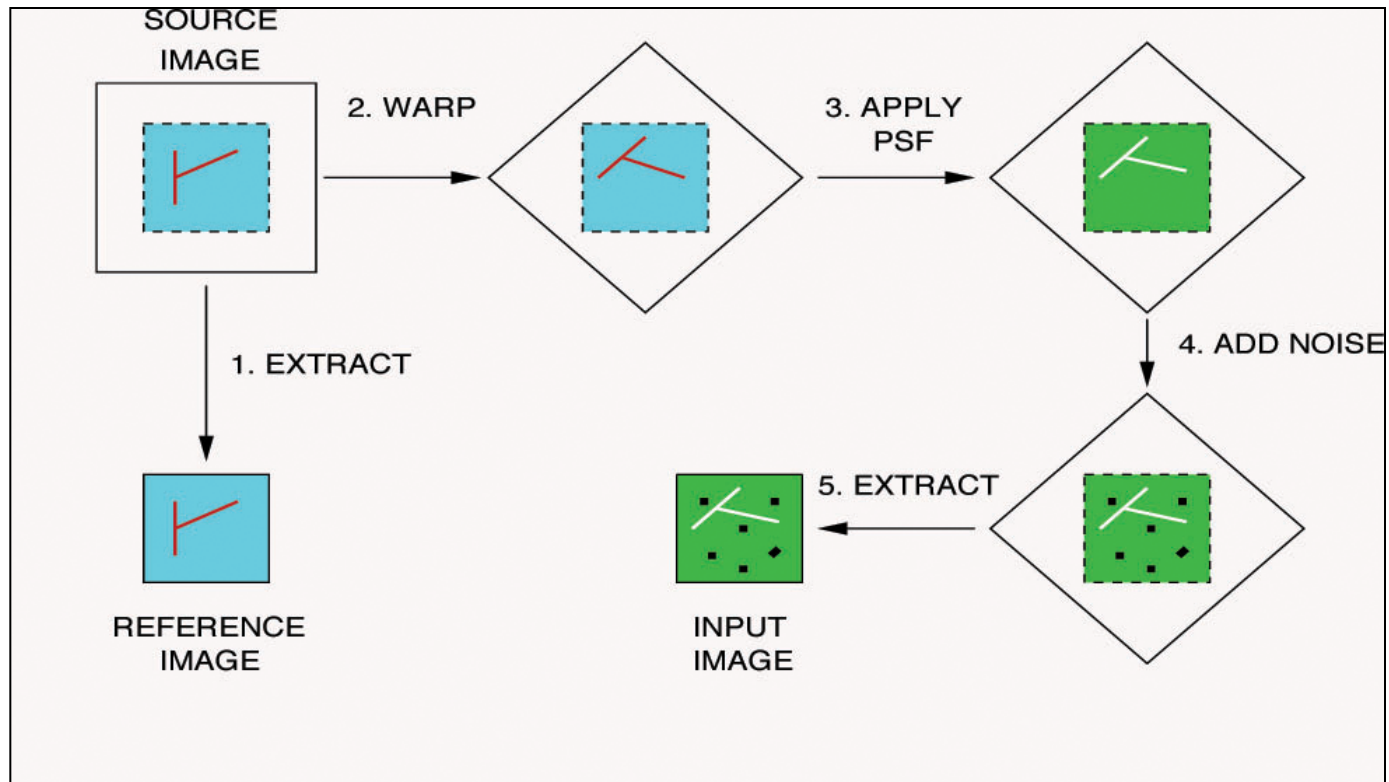
- Study of rotation- and translation-invariant wavelet filters (Spline, Simoncelli)
- Study of different matching strategies and metrics
- Parallel implementations (SIMD/MasPar, Beowulf Cluster, MIMD/Cray-T3E, FPGA-Hybrid)
- Development of image registration framework based on Brown's framework

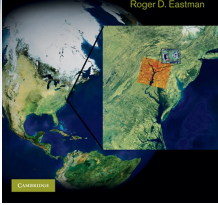




Experiments ... Datasets (1)

- Synthetic Data Experiments

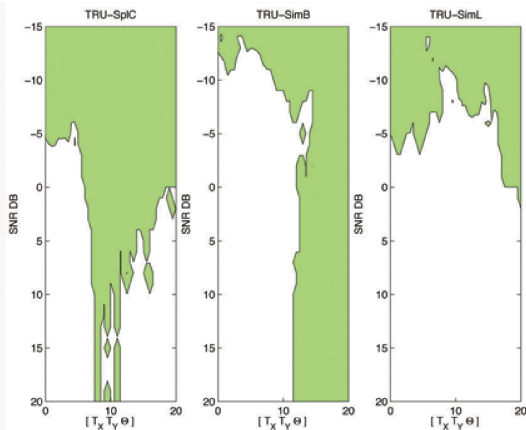




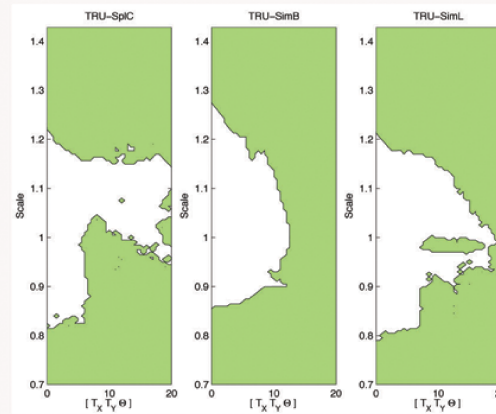
Experiments (1) ... Analysis Samples

- Various Features; Convergence as a function of noise and radiometric variations

(white areas – regions of convergence with errors less than threshold, e.g. 0.5)

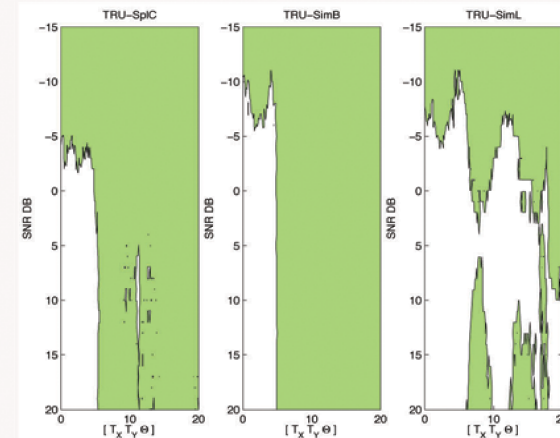


Warping + Noise



Warping + PSF

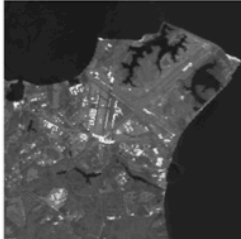
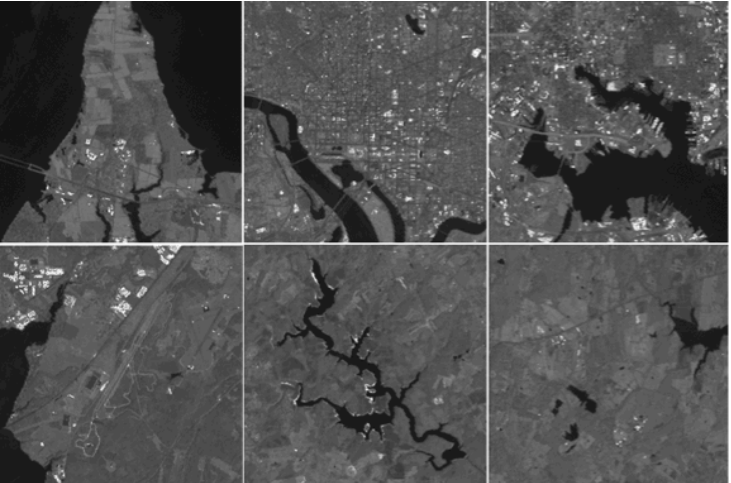
- Simoncelli-based methods outperform Spline pyramid-based methods
- Optimization based on Mutual Information does not perform better than L2-Norm
- Simoncelli-LowPass better than Simoncelli-BandPass for Low Noise and Same Radiometry and for Initial Guess Sensitivity



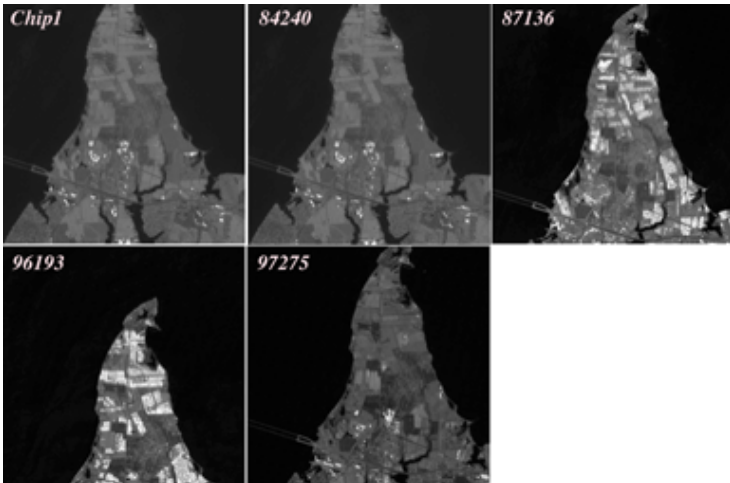
Warping + PSF + Noise

Experiments ... Datasets (2)

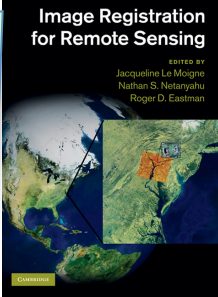
- Multi-Temporal Data
 - Landsat-5 and -7 (chips and corresponding windows)



7 Landsat chips



*1 Landsat chip
and 4 corresponding windows*

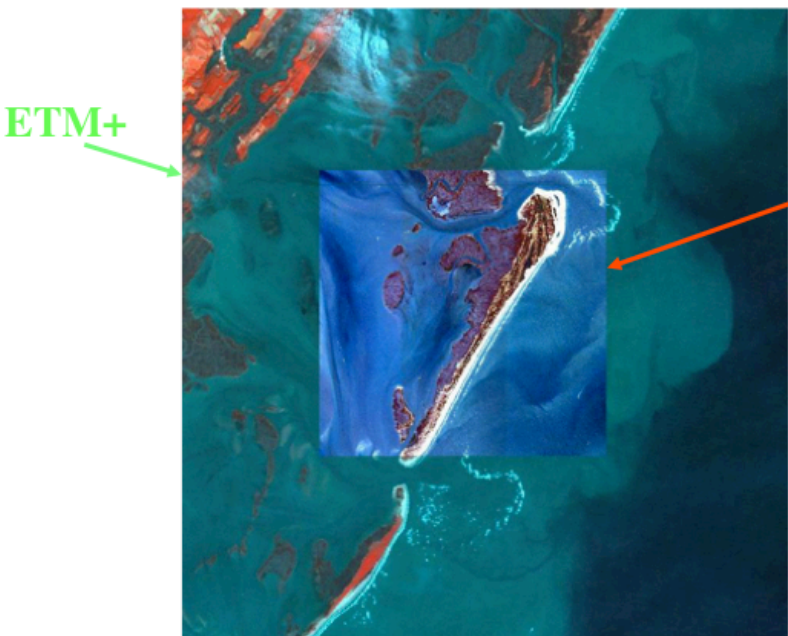


Experiments ... Datasets (3)

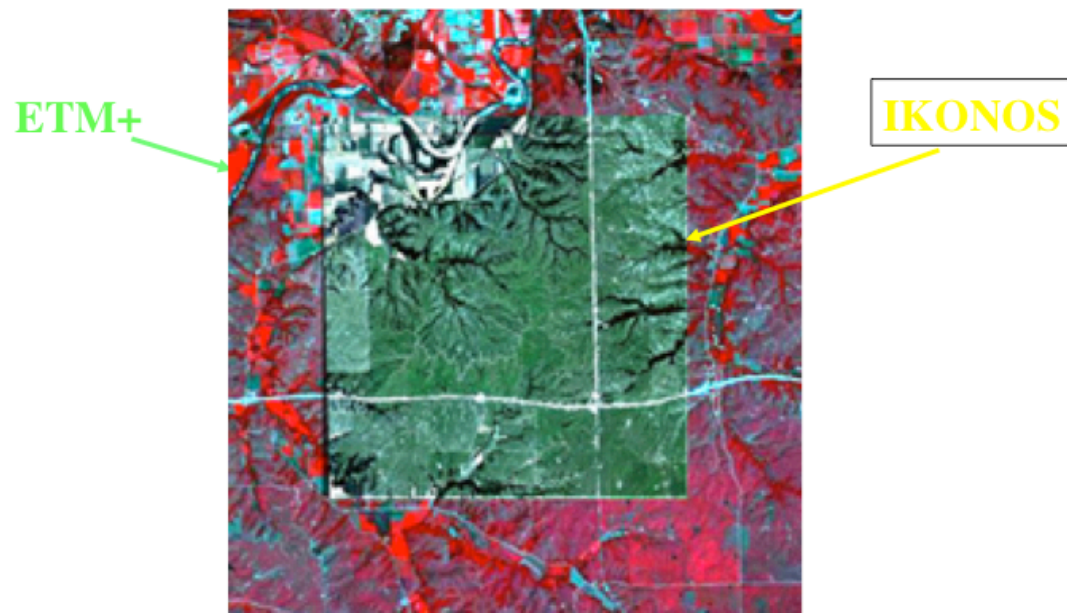
- Multi-Sensor Data
 - EOS Validation Core Sites
 - IKONOS/Landsat-7/MODIS/SeaWiFS
 - **Red and NIR** bands for each sensor
 - **Spatial resolutions:** IKONOS: 4m; ETM+: 30m; MODIS: 500m; SeaWiFS: 1000m
 - 4 different sites:
 - **Coastal Area:** VA, Coast Reserve Area, October 2001
 - **Agriculture Area:** Konza Prairie in State of Kansas, July to August 2001
 - **Mountainous Area:** Cascades Site, September 2000
 - **Urban Area:** USDA Site, Greenbelt, MD, May 2001

Experiments ... Datasets (3)

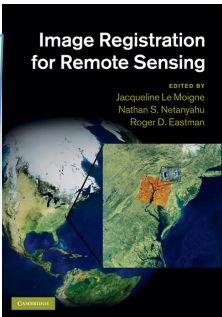
- Multi-Sensor Data



*ETM/IKONOS - Coastal
VA Data*



*ETM/IKONOS -
Agricultural Konza Data*



Experiments (2 and 3) ... Analysis Samples

Scene	RFM REGISTRATION			MANUAL GROUND TRUTH			ABSOLUTE ERROR		
	Q	T _x	T _y	Q	T _x	T _y	DQ	DT _x	DT _y
840827	0.031	4.72	-46.88	0.026	5.15	-46.26	0.005	0.43	0.62
870516	0.051	8.49	-45.62	0.034	8.58	-45.99	0.017	0.09	0.37
900812	0.019	17.97	-33.36	0.029	15.86	-33.51	0.010	0.11	0.15
960711	0.049	8.34	-101.97	0.031	8.11	-103.18	0.018	0.23	1.21

Global transformation vs. manual registration (or "ground truth") parameters for 4 Scenes in DC mutitemporal dataset

Image Name	Computed X	Computed Y	Comes from Registered Pair
IKONOS red	0	0	(Starting Point)
IKONOS nir	-0.2500	-0.2500	IKO red to ETM red and ETM red to IKO nir
IKONOS nir	-0.2500	-0.3125	IKO red to ETN nir and ETM nir to IKO nir

Self-Consistency Study of the Mutual Information Results


# of CVce Out of 32	TRU			TRUMI			SPSA			FCC
	SplC	SimB	SimL	SplC	SimB	SimL	SplC	SimB	SimL	
0.0	7	5	12	10	2	14	5	3	7	30
0.1	8	4	14	8	4	12	5	4	11	30
0.2	8	6	16	8	7	15	7	5	15	30
0.3	8	8	16	11	6	19	11	12	17	30
0.4	10	14	21	10	9	17	16	16	20	30
0.5	15	19	25	15	12	21	17	17	24	30
0.6	16	23	27	15	16	25	22	26	27	30
0.7	22	26	28	20	26	29	24	27	28	30
0.8	24	31	31	27	28	30	31	29	32	30
0.9	30	32	31	29	32	31	32	32	32	30
1.0	31	32	31	32	32	31	32	32	32	30

Number of cases that converge (out of 32) for the DC dataset, running 4 algorithms and different features with the initial guess varying between the origin (d=0.0) and ground truth (d=1.0)

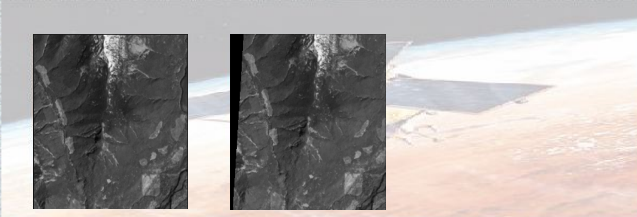
GOAL: DEFINE A "REGION OF CONVERGENCE" AND A "REGION OF DIVERGENCE" FOR EACH ALGORITHM
 → RECOMMENDATION FOR UTILIZATION OF ALGORITHMS AND ITS COMPONENTS



Toolbox for Registration and Analysis (TARA)

 **Web-based Image Registration**

[Tutorial](#)
[Contact Us](#)



1. Open Image files

Input Image:

Reference Image:


2. Select Registration Algorithm

UREG
 TRUMI
 SPSA
 Use All Algorithms

3. Customize Algorithm

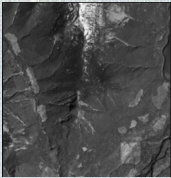
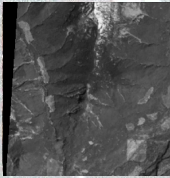
▾

4. Perform Registration

 **Web-based Image Registration**

[Tutorial](#)
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Successful Completion!

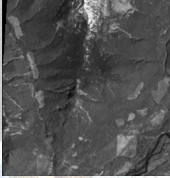
Reference Image  Input Image 

Parameters Selected
Rows = 256; Columns = 256; Wavelet Type = Spline

Result:

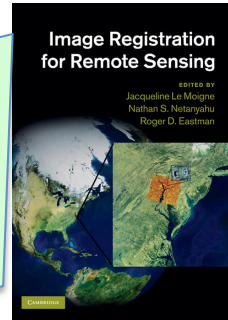
```

Translation coefficients:
Rotation angle = 4,000000
Shift_x = 5,000000
Shift_y = 2,000000
Scale_x = 1,000000
Scale_y = 1,000000
    
```

Output Image 

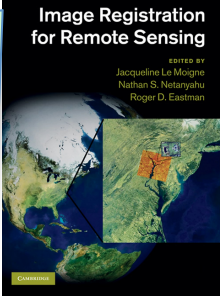
Copyright 2005, Code 606.3, NASA/Goddard Space Flight Center, Greenbelt, Maryland, USA.

THE BOOK ...

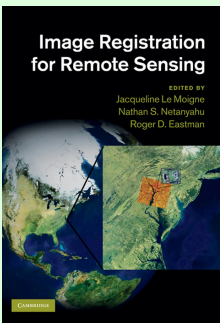


- *Image Registration for Remote Sensing*, ed. J. Le Moigne, N.S. Netanyahu and R.D. Eastman, Cambridge, UK:Cambridge University Press
- Foreword by Jón A. Benediktsson
- **Contributors:** S. Baillarin/CNES; D.G. Baldwin/Univ. of Colorado; M. Bernard/SPOT Image; A. Bouillon/Institut Géographique National; J.L. Carr/Carr Astronautics; R. Chellappa/UMD; Q-S. Chen/Hickman Cancer Center; A. Cole-Rhodes/Morgan State Univ.; R.I. Crocker/Univ. of Colorado; R. Davies/Univ. of Auckland; D.J. Diner/NASA JPL; W.J. Emery/Univ. of Colorado; A.A. Goshtasby/Wright State Univ.; V.M. Govindu/Indian Institute of Science; V.M. Jovanovic/NASA JPL; C.S. Kenney/UC Santa Barbara; B.S. Manjunath/UC Santa Barbara; J. Morisette/USGS; D.M. Mount/UMD; M. Nishihama/Raytheon @NASA GSFC; F.S. Patt/SAIC @NASA GSFC; S. Ratanasanya/form. UMD; K. Solanki/UC Santa Barbara; H.S. Stone/form. NEC Research Lab; J. Storey/SGT @USGS; S. Sylvander/CNES; B. Tan/ERT @NASA GSFC; P.K. Varshney/Syracuse Univ.; R.E. Wolfe/NASA GSFC; C. Woodcock/Boston Univ.; M. Xu/Syracuse Univ.; I. Zavorin/form. UMBC@NASA GSFC; M. Zuliani/UC Santa Barbara

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- *Part V – Conclusion and the Future of Image Registration*

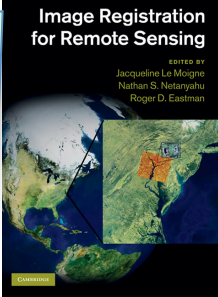


Feature Matching

Feature (Extraction), Similarity Metrics,
Transformations, and Matching Strategies

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Problem Statement

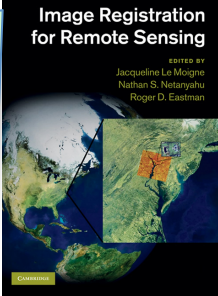
- Given a *reference* image, $I_1(x, y)$, and a *sensed* image $I_2(x, y)$, find the mapping (T_p, g) which “best” transforms I_1 into I_2 , i.e.,

$$I_2(x, y) = g(I_1(T_p(x, y), T_p(x, y))),$$

where T_p denotes spatial mapping and g denotes radiometric mapping.

- **Spatial transformations:**
 - Translation, rigid, affine, projective, perspective, polynomial
- **Radiometric transformations (resampling):**
 - Nearest neighbor, bilinear, cubic convolution, spline

Feature (Extraction)



- Gray levels
- Salient points
 - Edge-like, wavelet coefficients (Simoncelli and Freeman '95)
 - Corners (Kearny *et al.* '87, Harris and Stephens '88, Shi and Tomasi '94)
- Lines
- Contours, regions (Govindu *et al.* '99)
- Scale invariant feature transform (SIFT), Lowe '04

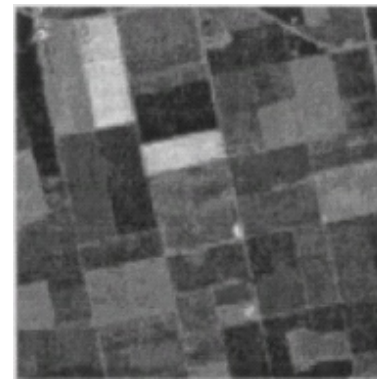


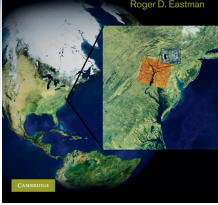
Similarity Metrics

- **L_2 -norm:**

- Minimize the sum of squared errors (SSD) over overlapping subimage

$$SSD(x, y) = \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} [I_1(m, n) - I_2(m - x, n - y)]^2$$





Similarity Metrics (cont'd)

- **Cross-correlation**

- Maximize *cross-correlation* over image overlap

$$I_1(x, y) \circ I_2(x, y) = \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} I_1(m, n) I_2(x + m, y + n)$$

- **Normalized cross-correlation (NCC)**

- Maximize normalized cross-correlation

$$NCC_{I_1, I_2}(x, y) = \frac{\sum_{m=0}^{M-1} \sum_{n=0}^{N-1} [I_1(m, n) - \bar{I}_1] [I_2(x + m, y + n) - \bar{I}_2]}{\sqrt{\sum_{m=0}^{M-1} \sum_{n=0}^{N-1} [I_1(m, n) - \bar{I}_1]^2 \cdot \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} [I_2(x + m, y + n) - \bar{I}_2]^2}}$$

Similarity Metrics (cont'd)

- **Mutual information (MI):**

Maximizes the degree of statistical dependence between the images

$$MI(I_1, I_2) = \sum_{g_1} \sum_{g_2} p_{I_1, I_2}(g_1, g_2) \cdot \log \left(\frac{p_{I_1, I_2}(g_1, g_2)}{p_{I_1}(g_1) \cdot p_{I_2}(g_2)} \right),$$

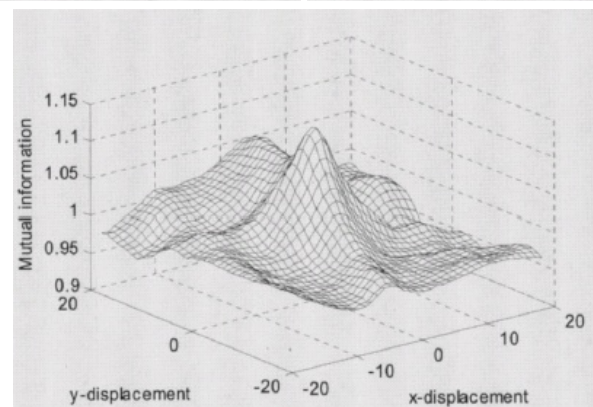
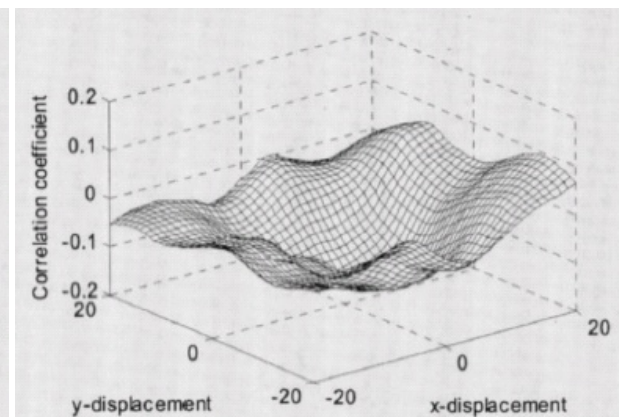
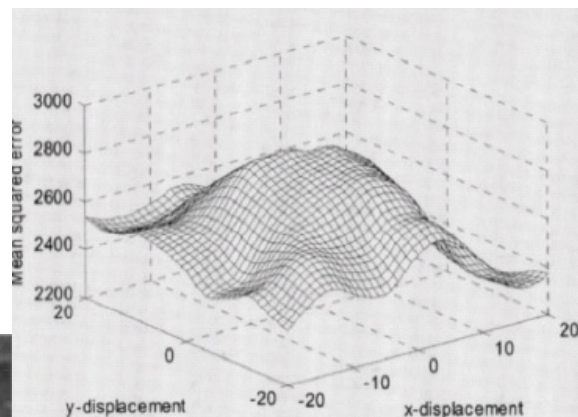
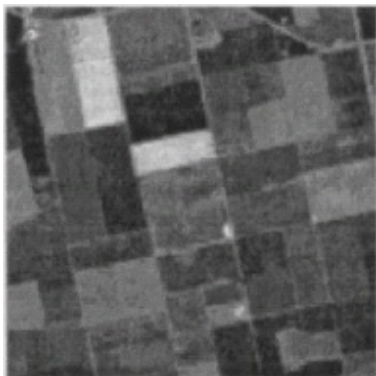
or using histograms, maximizes

$$MI(I_1, I_2) = \frac{1}{M} \sum_{g_1} \sum_{g_2} h_{I_1, I_2}(g_1, g_2) \cdot \log \left(\frac{M h_{I_1, I_2}(g_1, g_2)}{h_{I_1}(g_1) \cdot h_{I_2}(g_2)} \right)$$

where M is the sum of all histogram entries, i.e., number of pixels (in overlapping subimage)



Similarity Metrics (cont'd)



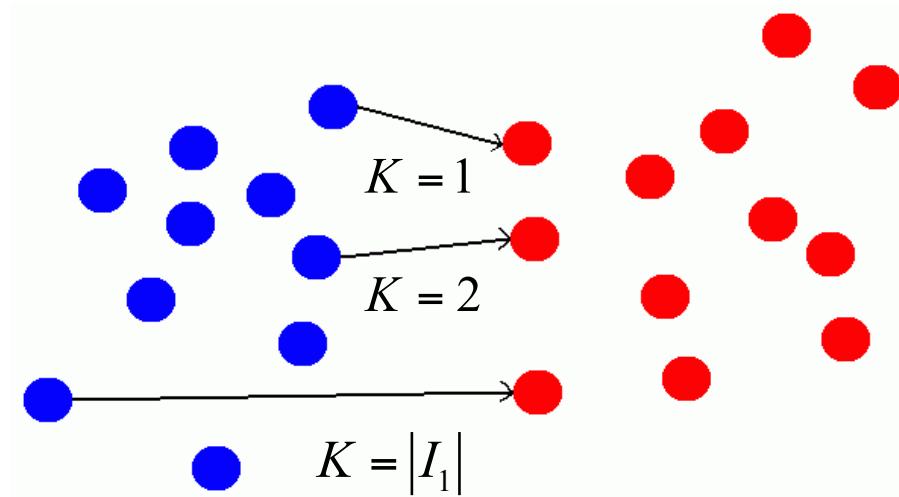
MI vs. L_2 -norm and NCC applied to Landsat-5 images (source: H. Chen *et al.* '03)

Similarity Metrics (cont'd)

- **Partial Hausdorff distance (PHD):**

$$H_K(I_1, I_2) = K^{th} \min_{p_1 \in I_1} \min_{p_2 \in I_2} \text{dist}(p_1, p_2),$$

where $1 \leq K \leq |I_1|$ (Huttenlocher *et al.* '93, Mount *et al.* '99)



Similarity Metrics (cont'd)

- **Discrete Gaussian mismatch (DGM):**

$$w_{\sigma}(a) = \exp\left(-\frac{\text{dist}(a, I_2)^2}{2\sigma^2}\right)$$

where $w_{\sigma}(a)$ denotes the *weight* of point a , and

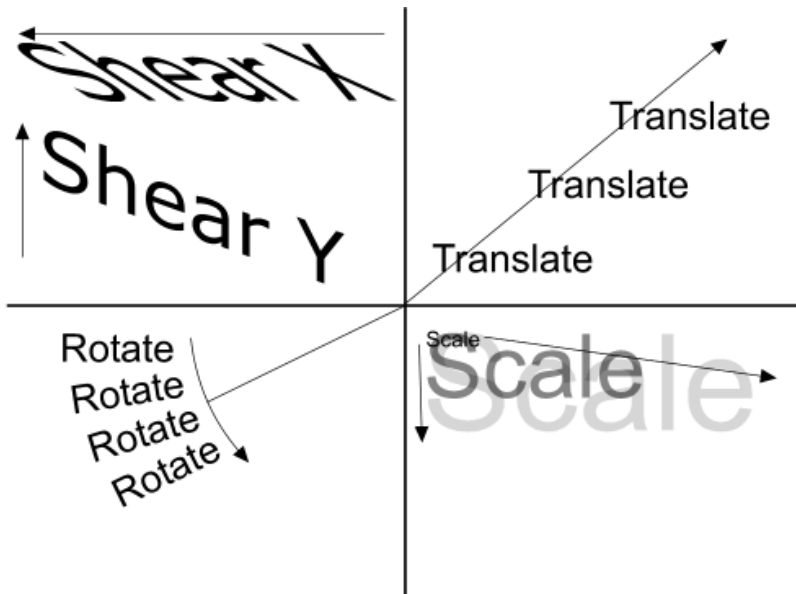
$$\text{DGM}_{\sigma}(I_1, I_2) = 1 - \frac{\sum_{a \in I_1} w_{\sigma}(a)}{|I_1|}$$

is similarity measure ranging between 0 and 1 (Mount *et al.*, Ch. 8)



Transformation Functions

- Translation-only, rigid
- Rotation, scale, and translation (RST)
- Affine (6 degrees of freedom)



$$x' = s \cos \theta \cdot x - s \sin \theta \cdot y + t_x$$

$$y' = s \sin \theta \cdot x + s \cos \theta \cdot y + t_y$$

$$T_p = \begin{pmatrix} s \cos \theta & -s \sin \theta & t_x \\ s \sin \theta & s \cos \theta & t_y \\ 0 & 0 & 1 \end{pmatrix}$$

- Projective/homography (e.g., for perspective effects in image mosaicing; Govindu and Chellappa, Ch. 10); 8 parameters

Transformation Functions (cont'd)

- Weighted linear transformation (Goshtasby, Ch. 7); adaptive transformation, continuous and smooth, applied to multiview images with *local geometric differences*, and maps an entire image to another
 - Interpolating surface is a weighted sum of planar patches, each of which passes through a *control point* and provides a desired gradient, i.e.,

$$f(x, y) = \frac{\sum_{i=1}^n R_i(x, y)L_i(x, y)}{\sum_{i=1}^n R_i(x, y)}$$

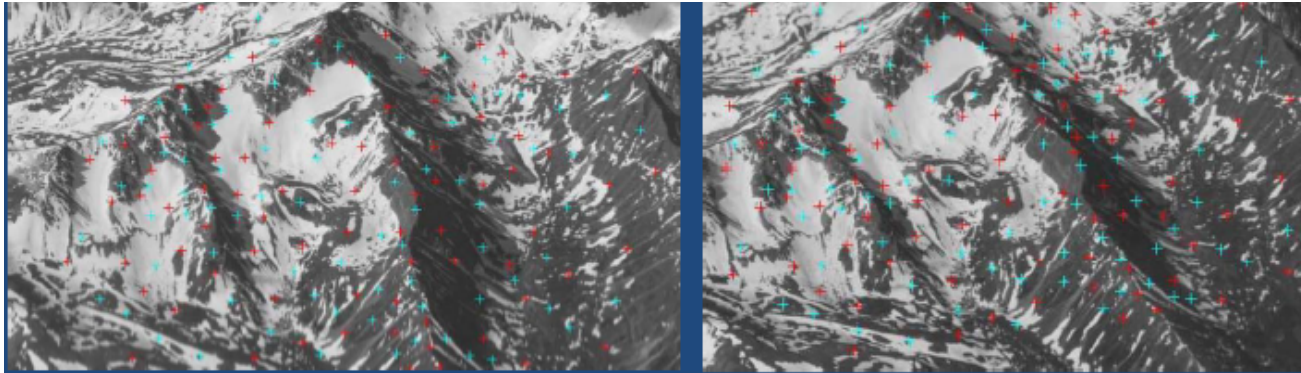
for monotonically decreasing weight $R_i(x, y) = \left[(x - x_i)^2 + (y - y_i)^2 \right]^{1/2}$

and

$$L_i(x, y) = a_i(x - x_i) + b_i(y - y_i) + F_i$$



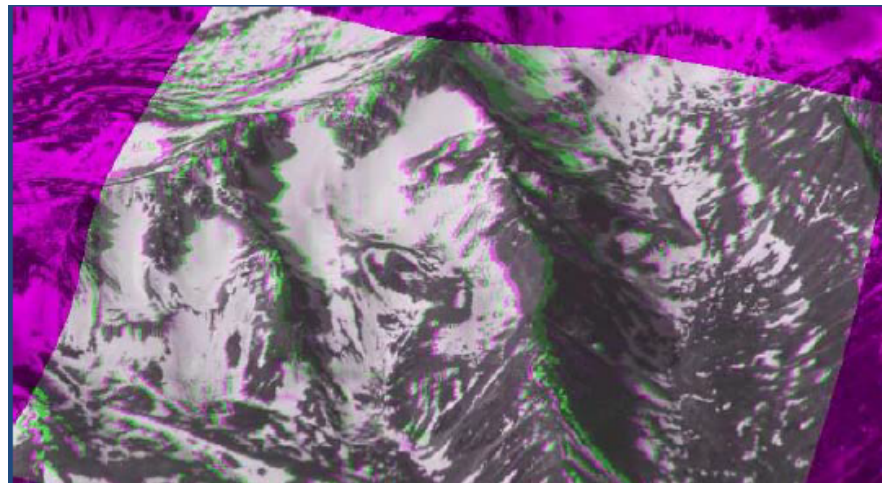
Transformation Functions (cont'd)



Reference

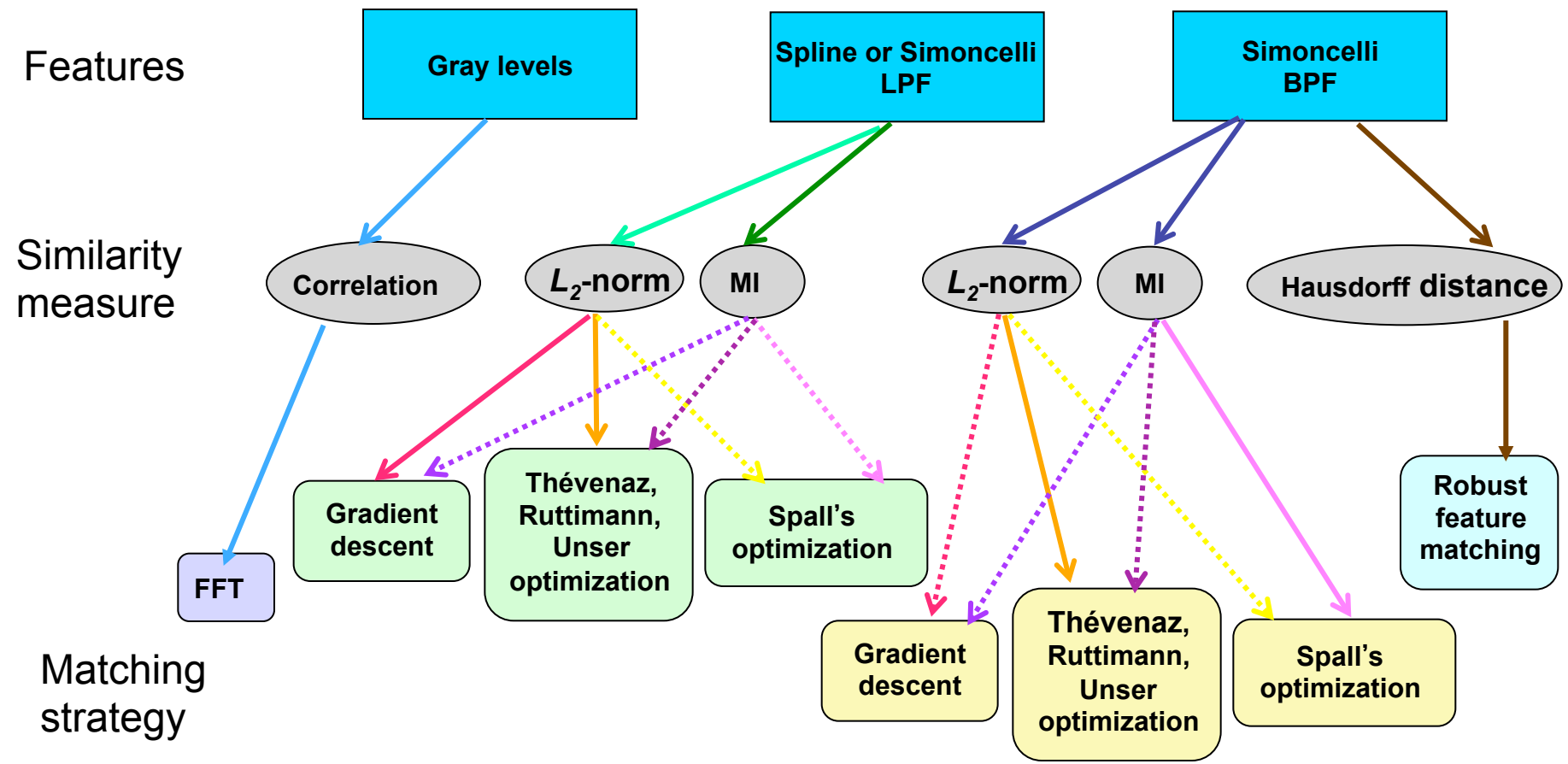
Sensed

Registered

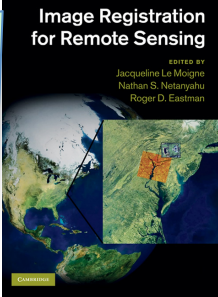


Source: Goshtasby, IR Tutorial, *CVPR '11*

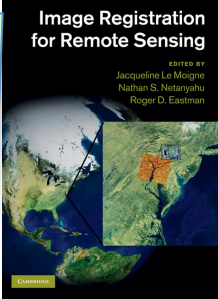
IR Components (Revisited)



Matching Strategies



- Exhaustive search (exponential in dimensionality of space)
- Fast Fourier transform (FFT)
- Numerical optimization (e.g., *steepest gradient descent* wrt SSD, NCC, and MI (Thévenaz, Ruttimann, and Unser (TRU) '98; Spall '92))
- Robust transformation estimate (e.g., RANSAC, LMS) if (most) correspondences are known (via SIFT-like)
- “Correspondenceless”, e.g., correlation of descriptor distribution/feature consensus (Govindu *et al.* '99)
- Robust feature matching (RFM), e.g., efficient subdivision and pruning of transformation space; Huttenlocher *et al.* '93, Mount *et al.* '99, Netanyahu *et al.* '04



Matching Strategies (cont'd)

- **Frequency domain-based approach (Stone, Ch. 4)**
 - Efficient computation of correlation as inverse of $F_1^*(u, v)F_2(u, v)$
 - Practical implementation (extension to NCC, masking invalid pixels, optimized computation)
 - Finding (small) rotational and scale differences (by matching chips)
 - Subpixel registration for translation-only using *phase* estimate (also in case of image aliasing)
 - Rotation and scale estimate by casting to *log-polar* coordinates

Matching Strategies (cont'd)

- **Matched filtering (Q. Chen, Ch. 5)**

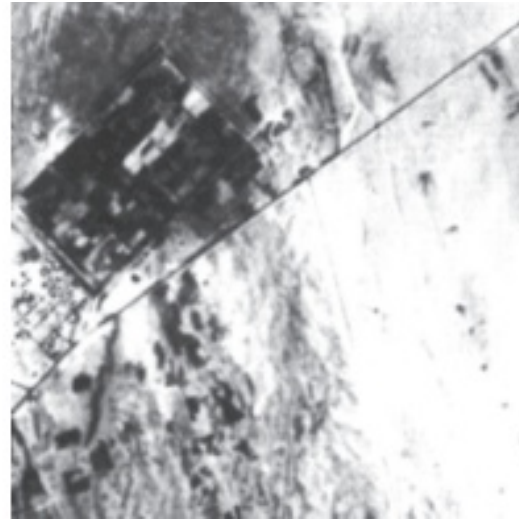
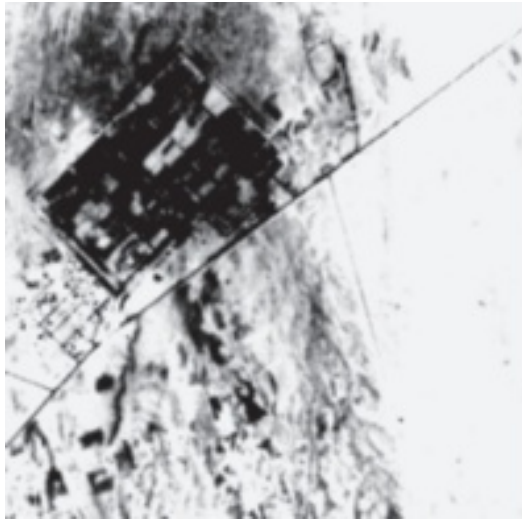
- Maximize SNR (using theory of linear systems)
- Apply *phase-only* and *symmetric phase-only* matched filters for translation-only IR

$$\text{Phase product} = \frac{F_1^*(u, v)}{|F_1(u, v)|} \frac{F_2(u, v)}{|F_2(u, v)|} = e^{-j(ut_x + vt_y)}$$

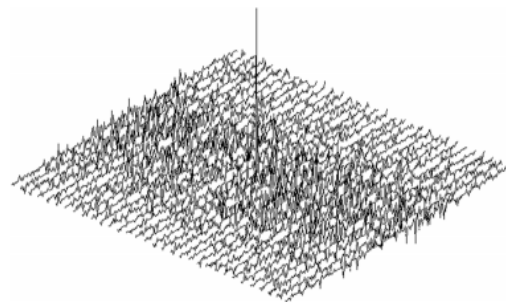
- Apply *Fourier-Mellin transform* for rotation and scale changes; transform represents these parameters as translational shifts in log-polar coordinates of magnitude of Fourier spectrum, i.e., first estimate rotation and scale, followed by translation estimate



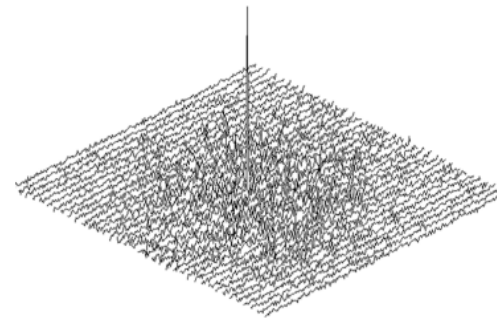
Matching Strategies (cont'd)



Rotation and
scale estimate



Translation
estimate



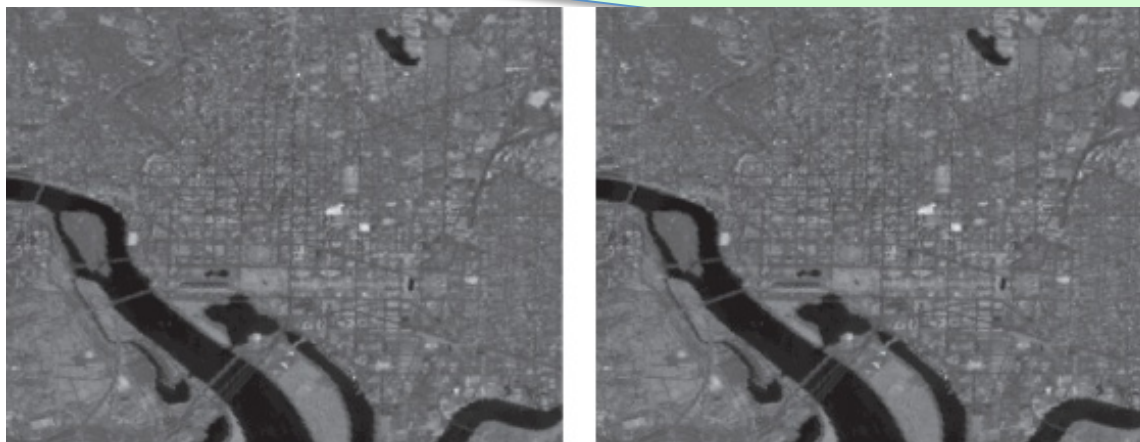
Pair of SPOT images and their registration, using symmetric phase-only matched filters on their Fourier-Mellin transforms

Matching Strategies (cont'd)

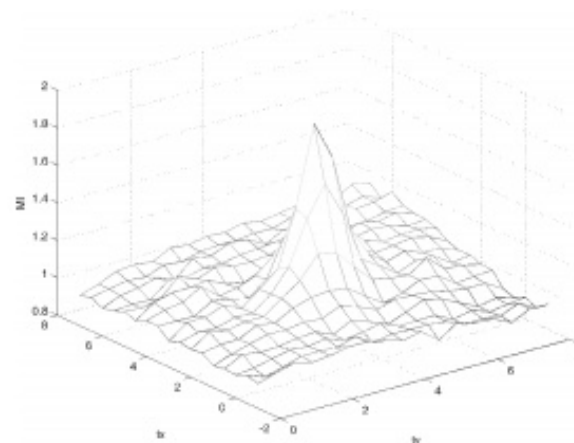
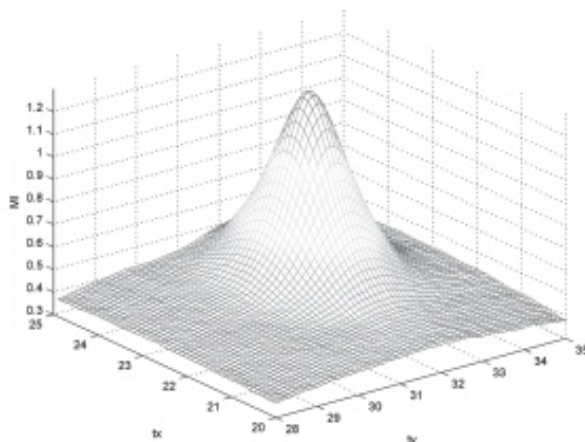
- **Numerical optimization** (Cole-Rhodes and Varshney, Ch. 6; Cole-Rhodes and Eastman, Ch. 12)
 - Powel's, Brent's (1-D), simplex, etc.
 - **Steepest descent/ascent variants**
 - Standard $\mathbf{p}_{k+1} = \mathbf{p}_k - \lambda_k \mathbf{g}_k$
 - Newton-Raphson $\mathbf{p}_{k+1} = \mathbf{p}_k - \lambda_k \mathbf{H}_k^{-1} \mathbf{g}_k$
 - Levenberg-Marquardt $\mathbf{p}_{k+1} = \mathbf{p}_k - (\mathbf{H}_k + \lambda_k \text{diag}[\mathbf{H}_k])^{-1} \mathbf{g}_k$
 - Apply to various similarity metrics, e.g., SSD (Eastman and Le Moigne '01), MI, etc.
 - » Explicit computation of gradient (and Jacobian/Hessian), e.g., Thévenaz and Unser '00
 - » Stochastic approx. (Spall '92); Cole-Rhodes *et al.* '03; Cole-Rhodes and Varshney, Ch. 6



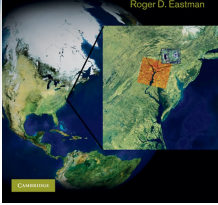
Matching Strategies (cont'd)



Pair of Landsat images over DC

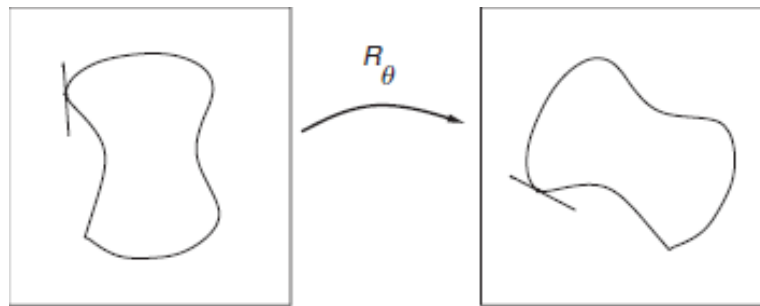


MI surfaces of above (level 1 and 4) images, using B-spline interpolation
(Cole-Rhodes and Varshney, Ch. 6)

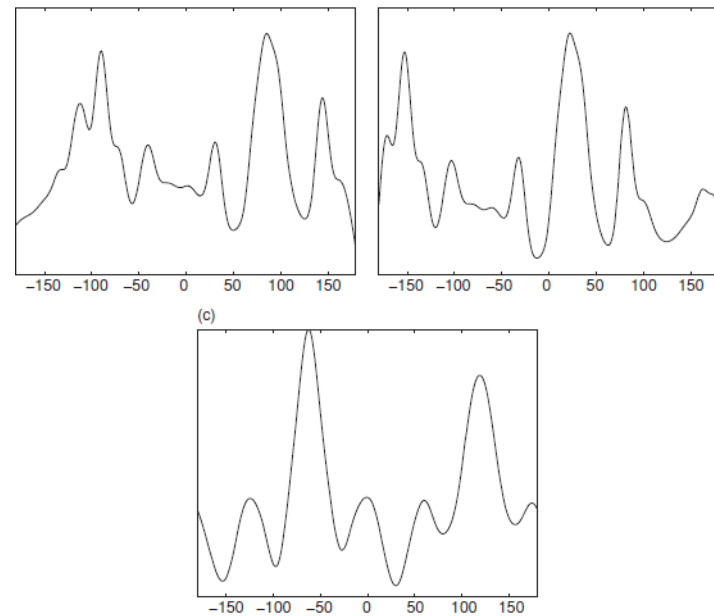


Matching Strategy (cont'd)

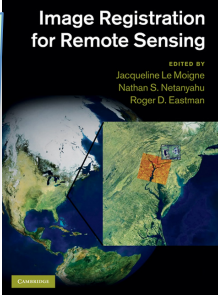
- **Alignment via local geometric distributions**
(Govindu and Chellappa, Ch. 10)



Rotated contours

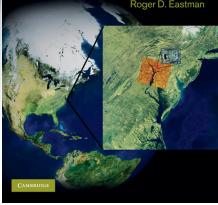


Slope angle distributions and their correlation

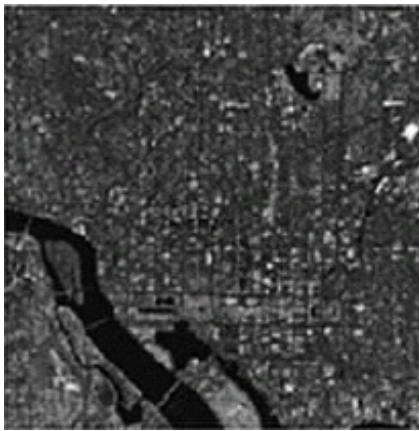
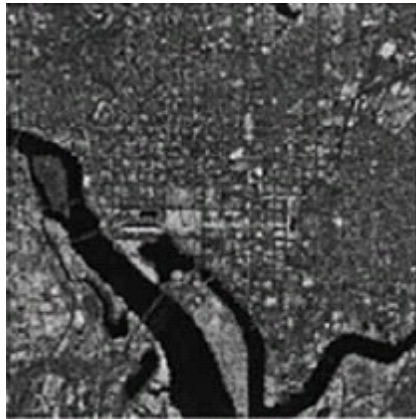


Matching Strategy (cont'd)

- **Robust feature matching (RFM)** (Mount *et al.*, Ch. 8)
 - **Space of affine transformations:** 6-D space
 - ***Subdivide*:** Quadtree or kd-tree. Each cell T represents a set of transformations; T is *active* if it may contain t_{opt} ; o/w, it is *killed*
 - ***Uncertainty regions (UR's)*:** Rectangular approximation to the possible images $\tau(a)$ for all $\tau \in T, a \in I_1$
 - ***Bounds*:** Compute *upper bound* (on optimum similarity) by sampling a transformation and *lower bound* by computing *nearest neighbors* to each UR
 - ***Prune*:** If lower bound exceeds best upper bound, then kill the cell; o/w, split it



Matching Strategy (cont'd)

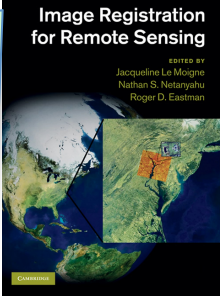


RFM-based registration of Landsat images over DC using wavelet features and PHD similarity measure (Netanyahu *et al.* '04)

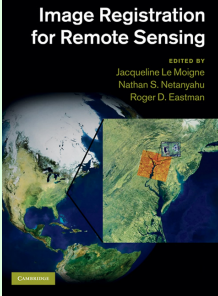
Matching Strategy (cont'd)

- **Computational efficiency**
 - “Culling” feature points via, e.g., *condition theory* (Kenney *et al.* '03, Ch. 9)
 - Efficient numerical or discrete algorithmic procedures
 - Hierarchical pyramid-like (wavelet) decomposition
 - Use landmark chip database (instead of a large scene) or alternatively, extract automatically corresponding regions of interest using *mathematical morphology* (Plaza *et al.* '05, '07)

Miscellaneous



- Use *Cramér-Rao bounds* as performance benchmark for performance evaluation of image registration (Xu and Varshney, Ch. 13)

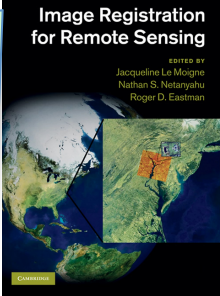


From Theory to Practice Operational Requirements

Roger D. Eastman

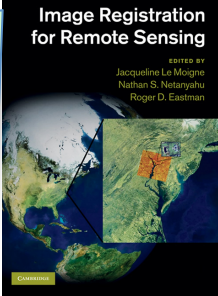
Loyola University, Baltimore,
Maryland

Why isn't this problem solved by now?



- A wealth of approaches!
- SIFT, ASIFT, BSIFT, SIFT/NCC, SIFT/FLOUR
- Beat the problem to death with terminology
- “Assume we have a Banach space ...”
- Many smart people wielding heavy mathematical weapons against a relatively fixed problem— why hasn't the problem yielded? Why no gold standard algorithm?

But it is solved ... ask LANDSAT



Operational Satellite Teams solve it every day

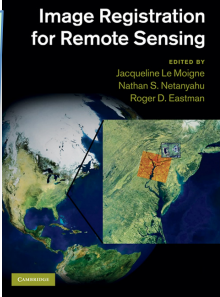
- GOES –Carr, Chapter 15
- MISR – Jovanovic et al, Chapter 16
- AVHRR – Emery et al, Chapter 17
- Landsat, Storey, Chapter 18
- SPOT, Ballarin, Chapter 19
- VEGETATION, Sylvander, Chapter 20
- MODIS, Wolfe et al, Chapter 21
- SeaWiFS, Patt, Chapter 22



And it's often solved the old-fashioned way (2008) – Normalized Cross Correlation

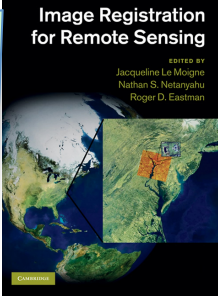
Instrument	Satellite	Resolution	Similarity	Subpixel
ASTER	Terra	15m-90m	NCC w/ DEM	Fit to surface
GOES	GOES I-M	1km-8km	NCC w/ vector coastlines	Bi-section search
MISR	Terra	275m	NCC w/ DEM	Least squares
MODIS	Terra	250m-1km	NCC w/ DEM	Fixed grid
HRS	SPOT	2.5m	NCC w/ DEM	Not described
ETM+	Landsat-7	15m-60m	NCC to arid region CPs	Fit to surface
VEGETATION	SPOT	1km	NCC w/ DEM	Not described

Example: Landsat ETM+



- Geodetic accuracy
 - Database of GCPs derived from USGS data
 - Normalized correlation
 - Updates navigation models
 - Results: RMSE $\sim 54\text{m}$
- Band-to-band registration
 - Selected tie-points in high-freq. arid regions
 - Normalized correlation
 - Subpixel by second order fit to 3×3 neighborhood
 - Result: 0.1 to 0.2 subpixel

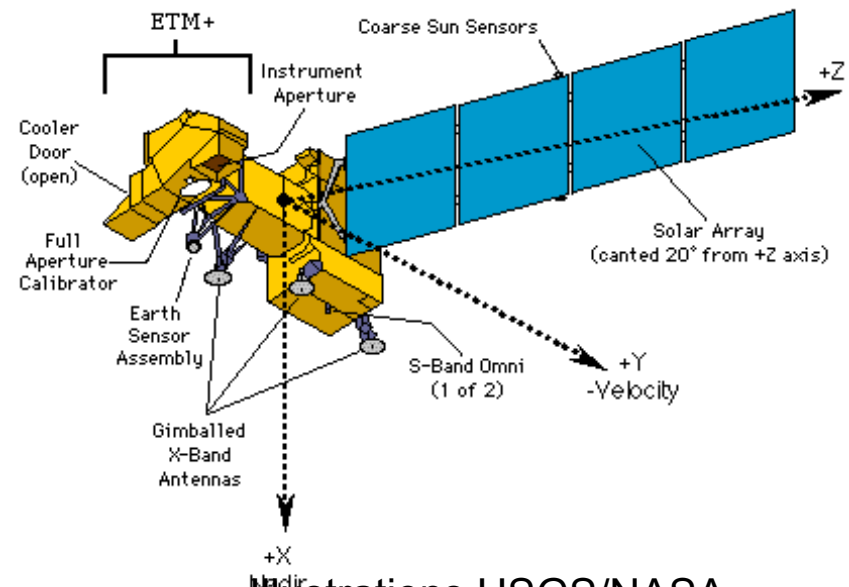
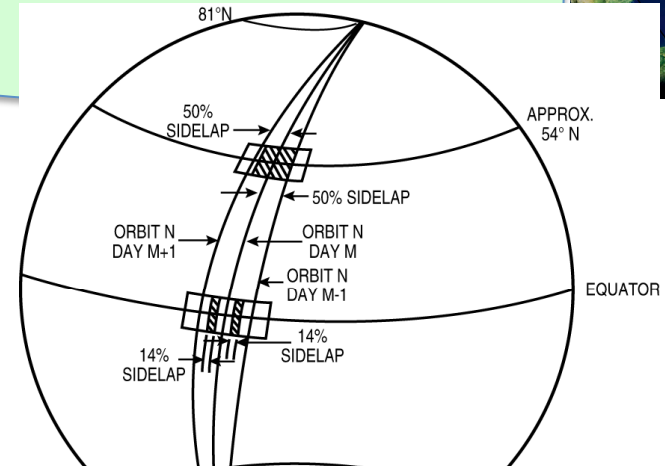
Operational teams requirements



- Know models of sensor/platform/
- Have access to complete data set
- Have continuing demands/responsibility
- Are registering same plots of land again and again – can invest effort in data preparation
- Can't take big risks on unproven methods

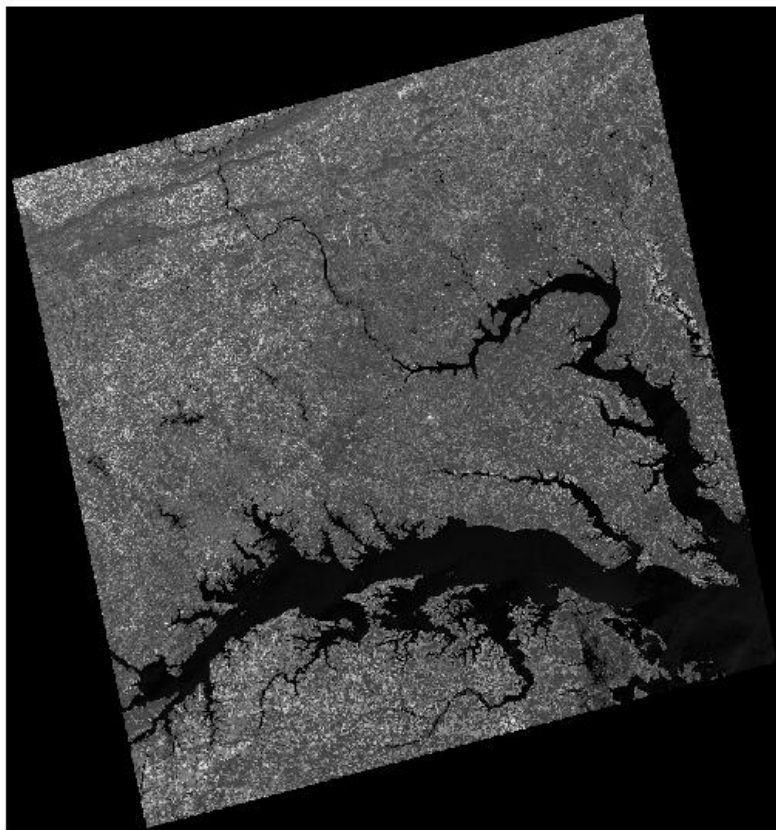
Know platform: Landsat team knowledge

- Sensor geometry
 - Band to band
- Sensor to platform
 - Sensor to sensor
- Orbit
 - Platform to Earth
- Terrain data
 - DEM
- Radiometric model



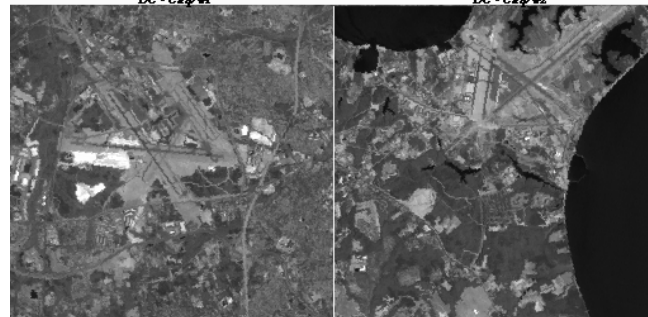
Illustrations USGS/NASA

Invest in data: ETM+ Chips



DC-Chip #1

DC-Chip #2



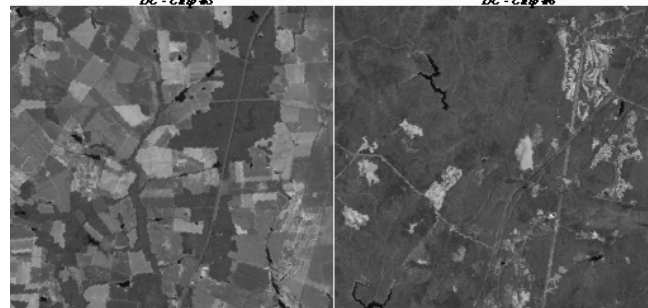
DC-Chip #3

DC-Chip #4



DC-Chip #5

DC-Chip #6



DC-Chip #7

DC-Chip #8

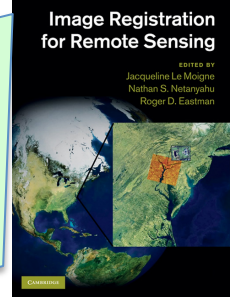
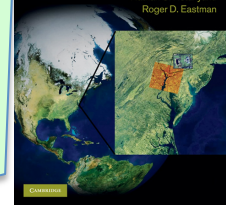


Image Registration
for Remote Sensing

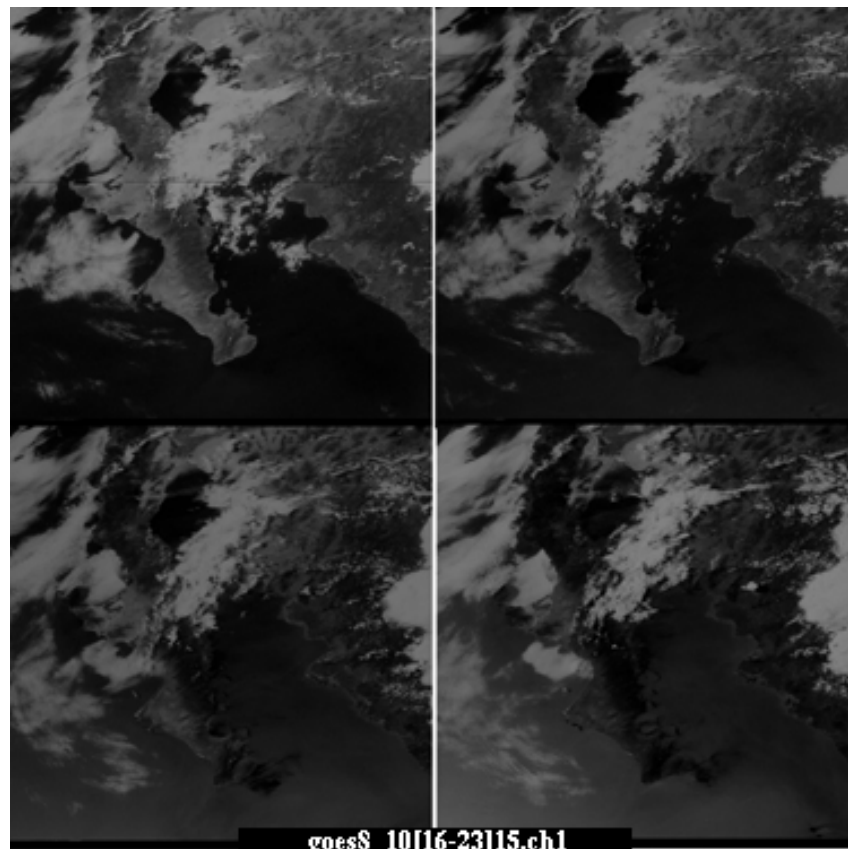
edited by
Jacqueline Le Moigne
Nathan S. Netanyahu
Roger D. Eastman

Copyright



Know data: GOES channel 1 (Baja)

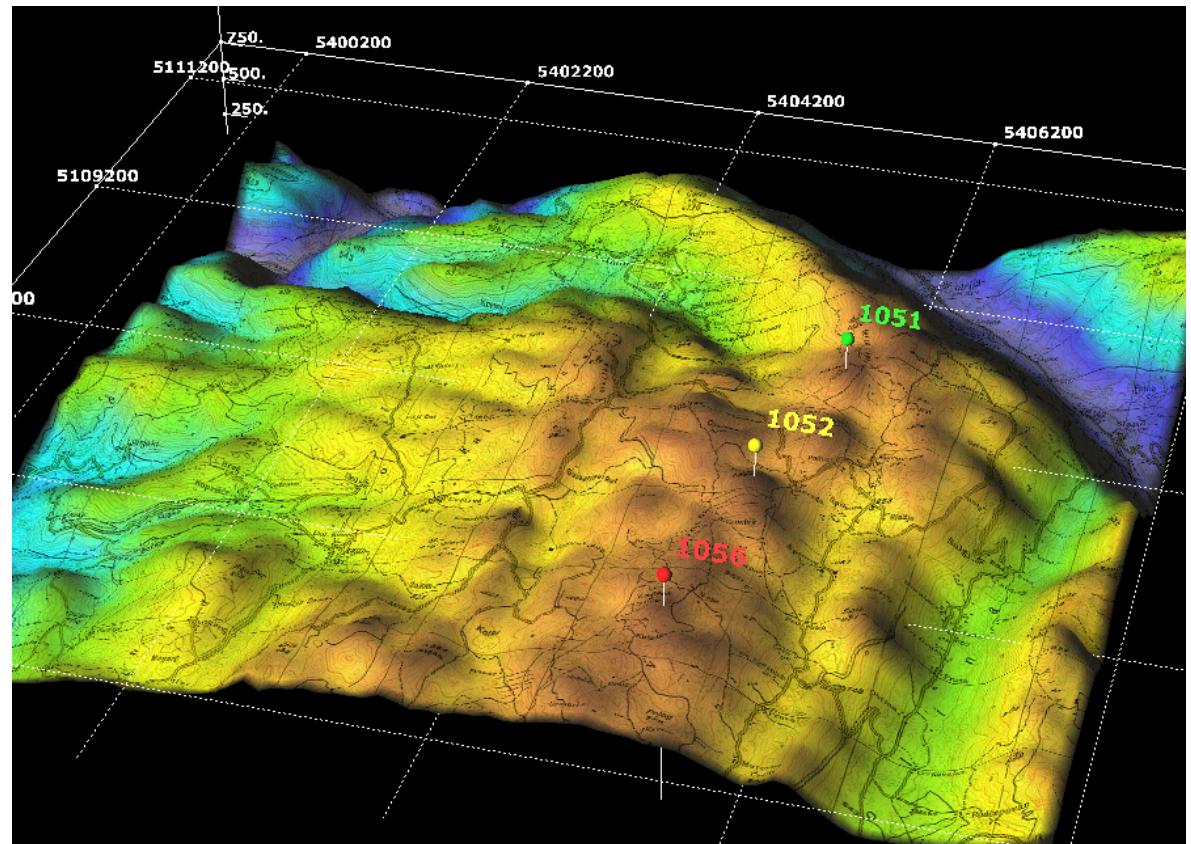
- Contrast reversal day to night
- Requires use of contour matching





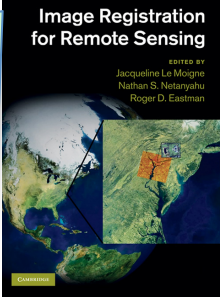
Use DEMs: Digital Terrain Models

Taking terrain into account in matching

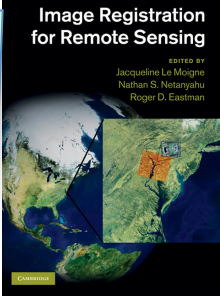


Use proven methods: Landsat 7 library

- Clean data, go fast
 - Use Normalized Grey-Scale Correlation
- Missing data/gaps, need robustness
 - Use Mutual Information
- Available alternative
 - Use Robust Feature Matching



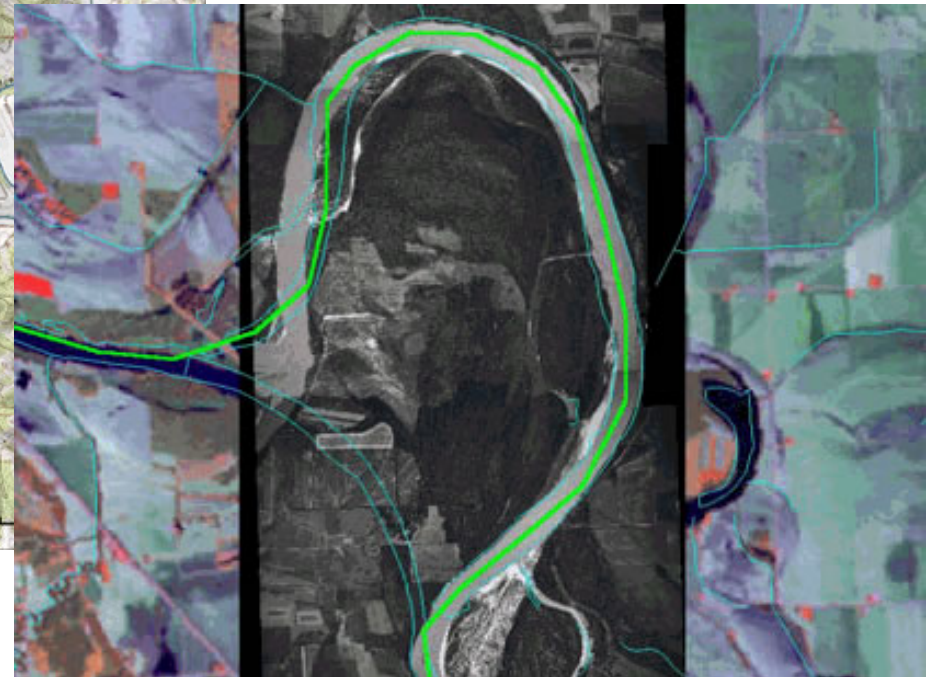
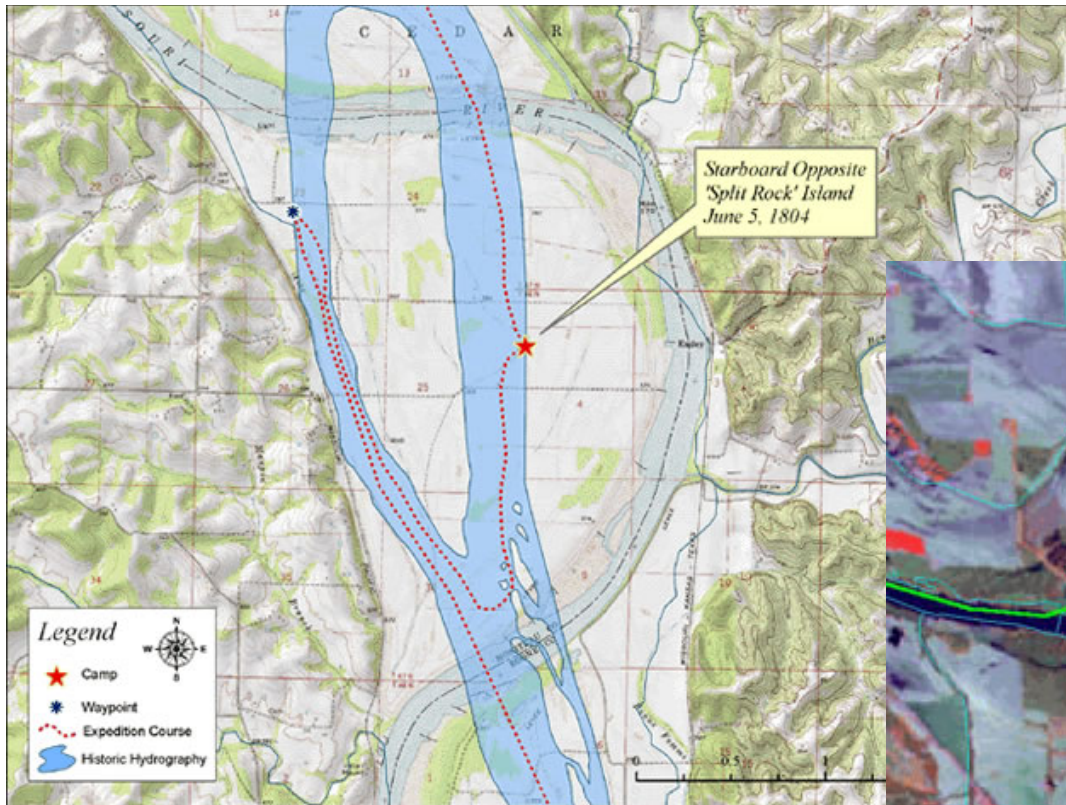
End Users – Earth scientists



- Know what data is for
- Have to fuse many data sets
- Have access to ancillary data
- Know cultural and historical data

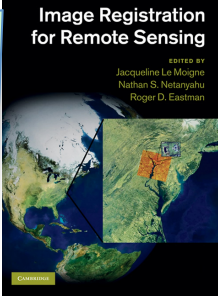
- Don't need one magic method – need toolbox of many approaches

Missouri river 1804-2002

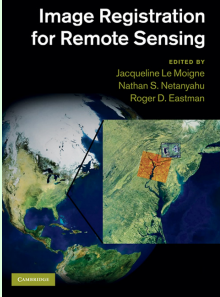


Illustrations U Missouri
Geography Department

Institutional challenges to “solving” IR for RS



- Different communities/literature/requirements
 - Photogrammetry
 - Computer vision/image processing
 - Operational teams
 - Remote sensing/Earth scientists/end users
- Demanding/varying mission requirements
 - Caution in system design, new methods
- Expensive sensors and images
 - Hard to share data or complete models



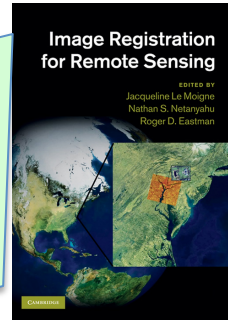
Conclusion

Jacqueline Le Moigne

Nathan S. Netanyahu

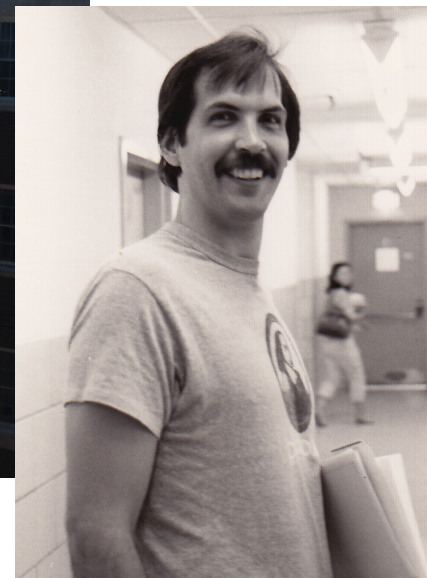
Roger D. Eastman

THE FUTURE OF IMAGE REGISTRATION

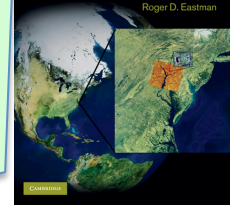


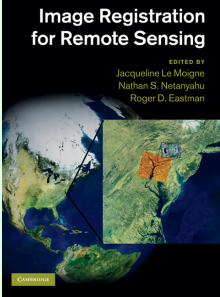
- **Satellite sensing/imaging in full expansion**
 - Explosion of commercial satellites
 - Exploring distant planets (Moon, Mars, etc.), e.g. Lunar Reconnaissance Orbiter (LRO)
- **Future research and challenges**
 - Combining multiple band-to-band registrations (e.g., hyperspectral data)
 - Automatically extracting windows of interest (decreasing processing time and increasing accuracy)
 - Dealing with other data sources (e.g., planetary imagery, or verification of optical systems)
 - Integration and fusion of multiple source imagery (various satellites, vector map, airborne, ground data, etc.)
 - Onboard implementations on specialized hardware
 - Multistage registration algorithms combining multiple principles and approaches and utilizing interdisciplinary systems engineering approach , thus increasing algorithms robustness and applicability

Other Memories, 1983 to 1988 ...



The Autonomous Land Vehicle (ALV) Project in Colorado...





Thank You!

Jacqueline Le Moigne

Nathan S. Netanyahu

Roger D. Eastman